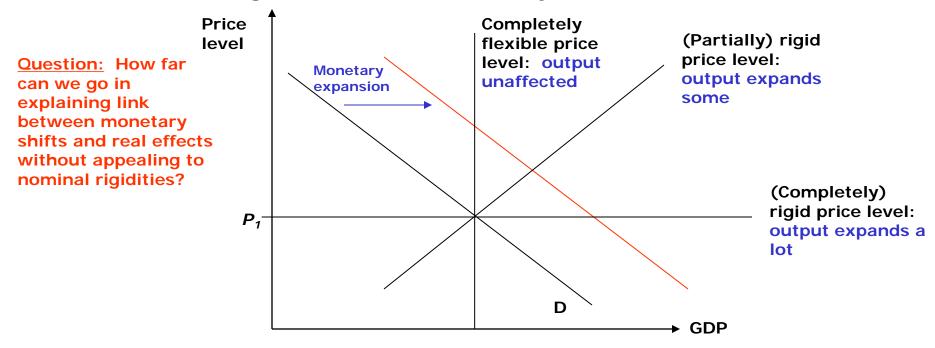
# SIMPLE DSGE MODELS OF "MONEY" PART II

# **OCTOBER 8, 2013**

- Stylized fact: high cyclical correlation of monetary aggregates and output
- Conventional Keynesian view: nominal rigidities (in price and/or wage level) cause monetary shifts to have real effects



#### Embed CIA framework in standard RBC model

- ...with quasi-linear utility...
- **Can approximate and simulate using "usual" methods** 
  - **Cooley and Hansen use LQ (linear-quadratic) approximation**...

Constant money growth rate; only z, shocks

		S. Time Series <sup>a</sup> 3–1984.1)	Economy with Constant Growth Rate $(\bar{g} = 0.99-1.15)^{\text{b}}$		
Series	Standard Deviation	Correlation with Output	Standard Deviation	Correlation with Output	
Output	1.74	1.00	1.76 (0.22)	1.00 (0.00)	
Consumption	0.81	0.65	0.51 (0.07)	0.87 (0.02)	
Investment	8.45	0.91	5.71 (0.74)	0.99 (0.00)	
Capital Stock	0.38	0.28	0.48 (0.09)	0.07 (0.07)	
Hours	1.41	0.86	(1.34)(0.18)	0.98 (0.00)	
Productivity	0.89	0.59	0.51 (0.07)	0.87 (0.03)	
Price Level ( CPI GNP Deflator	1.59 0.98	-0.48 - 0.53	0.51 (0.07)	- 0.87 (0.02)	

TABLE 1 — STANDARD DEVIATIONS IN PERCENT AND CORRELATIONS WITH OUTPUT FOR U.S. AND ARTIFICIAL ECONOMICS

> RATIO of SD(hours)/SD(productivity) = 2.6 – inherited from Hansen-Rogerson quasi-linear preferences....

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TABLE 1—STANDARD DEVIATIONS IN PERCENT AND CORRELATIONS WITH OUTPUT FOR U.S. AND ARTIFICIAL ECONOMICS

Business cycle dynamics same as Hansen (1985, Table 1)! Better be the case with the Friedman Rule (almost) in place!....BUT note they do not report dynamics of  $i_t$ ...

- **Exogenous AR(1) governs money growth rate** 
  - □ Set parameters (persistence and S.D. of shock) to match first and second moments of empirical *M*1 process

	Economy wit	money growth h Autoregressive te $(\bar{g} = 1.015)^{b}$	High average money growth Economy with Autoregressive Growth Rate ( $\bar{g} = 1.15$ ) <sup>b</sup>		
Series	Standard Deviation	Correlation with Output	Standard Deviation	Correlation with Output	
Output	1.73 (0.22)	1.00 (0.00)	1.74 (0.22)	1.00 (0.00)	
Consumption	0.62 (0.07)	0.72 (0.07)	0.65 (0.07)	0.70 (0.05)	
Investment	5.69 (0.76)	0.97 (0.01)	5.69 (0.77)	0.97 (0.01)	
Capital Stock	0.48 (0.10)	0.06 (0.07)	0.48 (0.10)	0.06 (0.06)	
Hours	1.33 (0.17)	0.98 (0.01)	1.33 (0.17)	0.98 (0.01)	
Productivity	0.50 (0.07)	0.87 (0.03)	0.50 (0.07)	0.87 (0.03)	
Price Level	1.70(0.34)	- 0.27 (0.16)	1.93 (0.27)	-0.25 (0.16)	

Result: volatility of nominal money reflected entirely in nominal prices and consumption

- **D** Makes some sense...the binding CIA constraint...  $c_t = \frac{M_t}{R}$
- Dynamics of other variables virtually unaffected

# **A PHILLIPS CURVE?**

- Tradeoff between inflation and unemployment the centerpiece of monetary theory and policy circa 1970
- □ Can CIA model deliver it?
  - Short-run Phillips Curve: No mention of cyclical correlation between π<sub>t</sub> and labor
  - Long-run (i.e., deterministic steady state) Phillips Curve: negative relation between inflation and employment
    - And thus with output, consumption, investment
    - □ (Steady-state!) inflation is a tax on consumption, hence substitute into leisure
- Empirical evidence may support "upward-sloping" *long-run* (i.e., steady state, i.e., *time-averaged*) Phillips Curve
  - But is this the same as the "...operational Phillips Curve..." (p. 745)? Likely not...

### WELFARE COSTS OF INFLATION

- Another enduring question: What are the welfare gains of moving from a high-inflation to a low-inflation environment?
  - Particular interest in this question in many developing countries and U.S. circa 1970-1980

Standard practice since Lucas (1987 *Models of Business Cycles*) Typical method: compute extra percentage of consumption representative agent would require in high-inflation environment to be just as well off (utility) as in low-inflation environment (without the consumption compensation)

#### $\Box$ Applied to steady state, compute $\zeta$ such that

$$\frac{u\left((1+\varsigma)\overline{c}^{\text{"BAD" POLICY}},\overline{n}^{\text{"BAD" POLICY}}\right)}{1-\beta} = \frac{u\left(\overline{c}^{\text{"GOOD" POLICY}},\overline{n}^{\text{"GOOD" POLICY}}\right)}{1-\beta}$$

"Consumption equivalents"

### WELFARE COSTS OF INFLATION

#### Cooley and Hansen results

TABLE 2—STEADY STATES AND WELFARE COSTS ASSOCIATED WITH VARIOUS ANNUAL GROWTH RATES OF MONEY

Define "good policy"			Annual Inflation Rate					
benchr	nar	k as Friedma	n Rule 🔶 🔸	-4	0.0	10	100	400
		Quarterly Cons	straint	Percent	Percent	Percent	Percent	Percent
			g =	β	1.0	1.024	1.19	1.41
		Steady State:	Output	1.115	1.104	1.077	0.927	0.783
			Consumption	0.829	0.821	0.801	0.690	0.582
			Investment	0.286	0.283	0.276	0.238	0.201
			Capital Stock	11.432	11.318	11.053	9.511	8.027
			Hours	0.301	0.298	0.291	0.250	0.211
	٢	Welfare Costs:	$\Delta C/C \times 100$	0.0	0.144	0.520	4.014	10.215
100 <b>ζ</b>	1		$\Delta C/Y \times 100$	0.0	0.107	0.387	2.984	7.596
	C	Monthly Const	raint					
			g =	β	1.0	1.008	1.06	1.12
		Steady State:	Output	0.387	0.386	0.383	0.364	0.345
		-	Consumption	0.286	0.285	0.283	0.269	0.255
			Investment	0.101	0.101	0.100	0.095	0.090
			Capital Stock	12.663	12.624	12.524	11.910	11.272
			Hours	0.303	0.302	0.300	0.285	0.270
_	٢	Welfare Costs:	$\Delta C/C \times 100$	0.0	0.040	0.152	0.981	2.137
100 <b>ζ</b>	1		$\Delta C/Y \times 100$	0.0	0.030	0.112	0.724	1.578

A common benchmark result in the literature – i.e., Lucas (2000), Lagos and Wright (2005), others compare with it

### WELFARE COSTS OF VARIABLE POLICY

□ Not studied by Cooley and Hansen

Typical method: compute extra percentage of consumption representative agent would require in variable-money-growth environment to be just as well off (utility) as in constantmoney-growth environment (without the consumption compensation)

 $\Box \qquad \text{Applied to dynamics, compute } \boldsymbol{\zeta} \text{ such that}$ 

$$\sum_{t=0}^{T} \beta^{t} u \left( (1+\varsigma) c_{t}^{\text{VARIABLE POLICY}}, n_{t}^{\text{VARIABLE POLICY}} \right) = \frac{u \left(\overline{c}^{\text{CONSTANT POLICY}}, \overline{n}^{\text{CONSTANT POLICY}}\right)}{1-\beta}$$

In practice, choose *T* large enough so that  $\beta^T \approx 0$ 

**Obtain** 
$$\{c_t, n_t\}_{t=0}^T$$
 through simulation

# **OTHER ANALYSIS**

In presence of other distorting taxes (labor- and capitalincome), welfare cost of moderate (long-run) inflation about double
TABLE 1

	Welfare and Revenue Consequences of Alternative Policies								
With other	Economy with Capital and Labor Income Taxation $\alpha = 0.84$								
distorting taxes (1991 <i>JMCB</i> )	Inflation Rate	Seigniorage	Seigniorage/ GNP	Welfare Cost of Inflation (%GNP)	Change in Total Revenue	Seigniorage/ Total Revenue	Welfare Cost of Policy (%GNP)		
	0.0 5.0 10.0 20.0 50.0	0.0 0.0094 0.0180 0.0333 0.0681	0.0 0.0083 0.0161 0.0304 0.0652	0.2794 0.6257 0.9628 1.6117 3.3860	0.0 0.0066 0.0126 0.0232 0.0463	0.0 0.0239 0.0448 0.0792 0.1464	16.843 17.259 17.664 18.443 20.575		
Without other	Economy with Only Inflation Tax								
distorting taxes (1989 <i>AER</i> )	Inflation Rate	Seigniorage	Seigniorage/ GNP	Welfare Cost of Inflation (%GNP)	Change in Total Revenue	Seigniorage/ Total Revenue	Welfare Cost of Policy (%GNP)		
	0.0 5.0 10.0 20.0 50.0	0.0 0.0143 0.0275 0.0508 0.1040	0.0 0.0077 0.0150 0.0282 0.0605	0.1048 0.2392 0.3751 0.6488 1.4661	0.0 0.0143 0.0275 0.0508 0.1040	1.0 1.0 1.0 1.0 1.0	0.1048 0.2392 0.3751 0.6488 1.4661		
	Economy with Capital and Labor Income Taxation $\alpha = 0.50$								
Also has revenue consequences (consolidated fiscal-monetary	Inflation Rate	Seigniorage	Seigniorage/ GNP	Welfare Cost of Inflation (%GNP)	Change in Total Revenue	Seigniorage/ Total Revenue	Welfare Cost of Policy (%GNP)		
budget) – basis for Ramsey models ala Lucas and Stokey (1983), Chari and Kehoe (1999)	0.0 5.0 10.0 20.0 50.0	0.0 0.0056 0.0107 0.0198 0.0405	0.0 0.0049 0.0095 0.0178 0.0374	0.1669 0.3719 0.5717 0.9556 1.9992	0.0 0.0039 0.0075 0.0138 0.0275	0.0 0.0143 0.0270 0.0485 0.0923	16.707 16.954 17.194 17.655 18.909		

#### SUMMARY

- Business cycle dynamics of real variables little-affected by exogenous fluctuations in money growth rate
  - Not a very strong "monetary propagation" mechanism
- Business cycle dynamics of nominal variables  $(\pi_t, i_t)$  not in line with empirical evidence (*Frontiers* chapter)
- □ Welfare costs of moderate (≈ 10 percent) long-run inflation ≈
   0.4 percent of long-run consumption
  - **Can double if economy is distorted by other taxes**
  - □ All stemming from (easing) the transactions (CIA) friction
    - New Keynesian models: source of welfare gains from lowering inflation (reduces relative-price distortions) very different
- Long-run upward-sloping Phillips Curve
  - New Keynesian models: emphasis on short-run Phillips Curve

## **OTHER GENERAL ISSUES**

- □ Which assets provide liquidity services?
  - □ Money
  - □ (Some) bonds?
  - Which to include in CIA constraint?
- □ Timing?
  - Do money/asset markets meet before or after goods markets?
  - Carlstrom and Fuerst (2001 JME) demonstrate precise timing of monetary models can be crucial for some results
- □ Money growth rules vs. interest rate rules?
  - **Non-New Keynesian models typically use money growth rule** 
    - But see Gavin, Kydland, and Pakko (2007 JME) for recent example using interest rate rule
  - New Keynesian models typically use interest rate rule