MONOPOLISTIC COMPETITION IN A DSGE MODEL: PART I

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EMPIRICAL AND THEORETICAL CONSIDERATIONS

- Evidence supports existence of markups in goods markets (i.e., p > mc)
 - □ Basu and Fernald (1997 JPE) often-cited source
- Evidence also supports positive (but small?...) pure economic profits
- □ Are firms always price-takers?
 - □ If not, must endow them with market power
- If increasing returns in production exist, a model without market power does not admit an equilibrium with increasing returns
- **Introduce imperfect competition**
 - **Typically monopolistic competition...**
 - …a building block of modern sticky-price models

WORKHORSE MODEL

□ Dixit-Stiglitz (1977 AER) model

- Most common specification of imperfect competition in macro models
- **(Near-) universal building block of modern sticky price models**
- □ Basic idea: imperfectly-substitutable goods combined yield an aggregate good

 ε the constant elasticity of substitution between any pair of differentiated goods

$$c_{t} = \left[\sum_{i=1}^{N_{t}} c_{it}^{\frac{\varepsilon-1}{\varepsilon}}\right]^{\frac{\varepsilon}{\varepsilon-1}}$$
$$c_{t} = \left[\int_{0}^{N_{t}} c_{t}(i)^{\frac{\varepsilon-1}{\varepsilon}} di\right]^{\frac{\varepsilon}{\varepsilon-1}}$$

Discrete number of differentiated goods

Continuum of differentiated goods

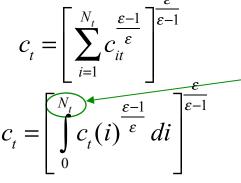
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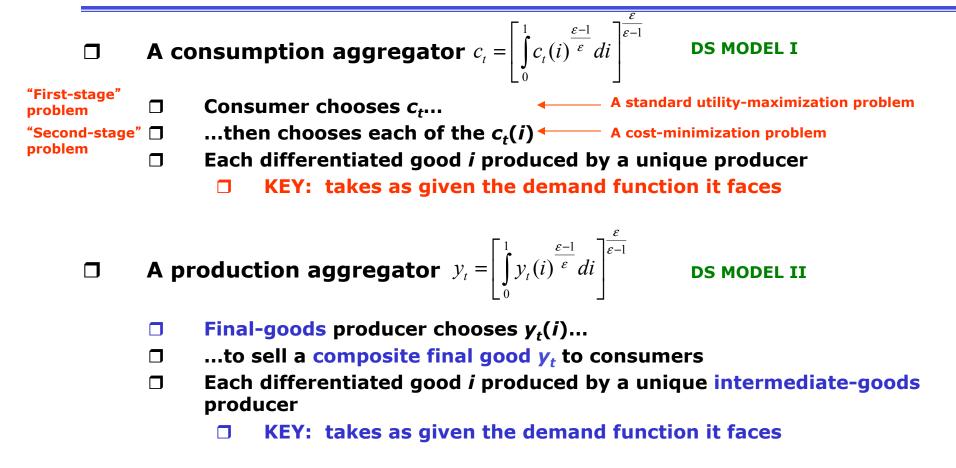
In some applications, make this endogenous and/or time-varying, N_t

Continuum of differentiated goods

- Important properties of aggregator
 - **Symmetric in all arguments**
 - **Strictly increasing in all arguments**
 - **Strictly concave in all arguments**
 - Homogenous of degree one

Drives efficiency/optimal policy results (later...)

TWO EQUIVALENT IMPLEMENTATIONS



MARKET ORGANIZATION



- Some fixed production factor –
 See Rotemberg and Woodford (*Frontiers* chapter) primarily useful for calibrating profit share for details on "materials cost" foundations
- Differentiated producer *i* hires inputs on perfectly-competitive markets...
- …and sells its output on its own *monopolistically-competitive* market
 - **Sells "directly" to consumers... DS MODEL I**
 - □ ...or to final-goods firms DS MODEL II
- **Common assumption:** $\phi = 0$ (\rightarrow mc = ac assuming CRS)

FINAL-GOODS FIRMS

DS MODEL II

(Representative) final goods producer

 $\max_{y_{it}} y_{t} - \int_{0}^{1} p_{it} y_{it} di$ NOTE: final output serving as numeraire Substitute in CES final-goods aggregator

$$\max_{y_{it} \downarrow_{i=0}^{1}} \left[\int_{0}^{1} y_{it}^{\frac{\varepsilon-1}{\varepsilon}} di \right]^{\frac{\varepsilon}{\varepsilon-1}} - \int_{0}^{1} p_{it} y_{it} di$$

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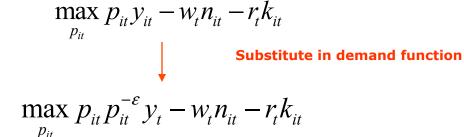
Takes as given all p_{it}

Profit-maximization leads to demand functions for each underlying differentiated good i

 $y_{it} = p_{it}^{-\varepsilon} \cdot y_t$ taken as given by differentiated firm *i* Each differentiated firm *i* chooses its *p*_{*i*} to maximize profit Relative price of firm *i*'s Aggregate output a shifter of firm i's demand function output

DS MODEL II

D Differentiated goods producer *i*



- □ A "two-stage" optimization problem
 - **Stage 1:** Choose optimal p_i

i.e., total production y_i is simply "read off the demand curve"

- □ (Intermediate "stage"): "choose" to produce the y_i corresponding to the optimal choice of p_i
- **Stage 2:** Choose factor inputs to produce y_i at minimum cost

DS MODEL II Differentiated goods producer *i* $\max p_{it} y_{it} - w_t n_{it} - r_t k_{it}$ Substitute in demand function $\max p_{it} p_{it}^{-\varepsilon} y_t - w_t n_{it} - r_t k_{it}$ p_{it} A "two-stage" optimization problem Stage 1: Choose optimal p_i i.e., total (Intermediate "stage"): "choose" to produce the y_i corresponding production y_i is to the optimal choice of p_i simply "read off the Stage 2: Choose factor inputs to produce y_i at minimum cost demand curve" GIVEN 1) CRS f(k, n) and 2) $\phi = 0$ \rightarrow mc = ac = CONSTANT (with respect to quantity) STAGE-1 $\max p_{it} p_{it}^{-\varepsilon} y_t - mc_t p_{it}^{-\varepsilon} y_t$ $\max p_{it} p_{it}^{-\varepsilon} y_t - mc_t y_{it} - m$ PROBLEM p_{it} p_{it} Substitute in demand function

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DS MODEL I or II

D Differentiated goods producer *i* optimal choice of p_i

$$p_{it} = \frac{\varepsilon}{\varepsilon - 1} \cdot mc_t$$

Gross product-market markup

Linked *only* to degree of substitutability

RBC model: ε = infinity (perf. comp.)

Monopoly model requires $\varepsilon > 1$ and $\varepsilon <$ infinity

DS MODEL I or II

 \Box Differentiated goods producer *i* optimal choice of p_i

$$p_{it} = \frac{\varepsilon}{\varepsilon - 1} \cdot mc_t$$

Gross product-market markup

Linked *only* to degree of substitutability

RBC model: ε = infinity (perf. comp.)

Stage 2: cost-minimization NOTE: cost-Monopoly model requires $\varepsilon > 1$ **Given** optimal (p_i, y_i) minimization and ε < infinity $\max_{k_{it}, n_{it}} p_{it} z_t f(k_{it}, n_{it}) - w_t n_{it} - r_t k_{it}$ equivalent to profitmaximization substitute $p_{it} = [z_t f(k_{it}, n_{it})]^{-1/\varepsilon} y_t^{1/\varepsilon}$ from dmd. fct. GIVEN (p_i, y_i) -i.e., DUAL PROBLEM $\max_{k_{it}, n_{it}} \left[z_t f(k_{it}, n_{it}) \right]^{1-1/\varepsilon} y_t^{1/\varepsilon} - w_t n_{it} - r_t k_{it}$ Factor demands (k_{ir}, n_i) solve $\frac{\varepsilon - 1}{\varepsilon} p_{it} z_t f_k(k_{it}, n_{it}) = r_t \qquad \frac{\varepsilon - 1}{\varepsilon} p_{it} z_t f_n(k_{it}, n_{it}) = w_t$

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BUILDING THE EQUILIBRIUM

DS MODEL I or II

Putting things together – impose symmetry across all *i*

$$\frac{\varepsilon - 1}{\varepsilon} p_t z_t f_k(k_t, n_t) = r_t \quad \& \quad \frac{\varepsilon - 1}{\varepsilon} p_t z_t f_n(k_t, n_t) = w_t \quad \& \quad p_t = \frac{\varepsilon}{\varepsilon - 1} \cdot mc_t$$

$$\lim_{t \to \infty} mc_t = \frac{w_t}{z_t f_n(k_t, n_t)} = \frac{r_t}{z_t f_k(k_t, n_t)}$$

BUILDING THE EQUILIBRIUM

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$$\frac{\varepsilon - 1}{\varepsilon} p_t z_t f_k(k_t, n_t) = r_t \quad \mathbf{a} \quad \frac{\varepsilon - 1}{\varepsilon} p_t z_t f_n(k_t, n_t) = w_t \quad \mathbf{a} \quad p_t = \frac{\varepsilon}{\varepsilon - 1} \cdot mc_t$$

$$\lim_{t \to \infty} mc_t = \frac{w_t}{z_t f_n(k_t, n_t)} = \frac{r_t}{z_t f_k(k_t, n_t)}$$

Symmetric equilibrium *relative price* of an intermediate good? Substitute demand functions into DS aggregator and compute...

$$p_t = 1$$

$$\downarrow$$

$$mc_t = \frac{\varepsilon - 1}{\varepsilon}$$

With measure one of intermediate firms, can think of as a normalization...but what if measure $[0, N_t]$ of firms?

< 1 with ε > 1 and ε < infinity

Monopoly power causes factor prices to fall below marginal products... hence inefficiently low equilibrium factor use...hence inefficiently low total output

MONOPOLISTICALLY-COMPETITIVE EQUILIBRIUM

- Equilibrium Conditions (symmetric across all differentiated goods)
 - **Consumption-leisure optimality condition**
 - **Consumption-savings optimality condition**
 - □ Aggregate resource constraint

$$c_t + k_{t+1} - (1 - \delta)k_t = z_t f(k_t, n_t)$$

□ (Market clearing in labor, capital, and goods markets)

$$\square \qquad mc_t = \frac{\varepsilon - 1}{\varepsilon} \quad \forall t \quad (< 1 \text{ with } \varepsilon > 1)$$

Factor prices a mark*down* of marginal products

$$w_t = \frac{\varepsilon - 1}{\varepsilon} \cdot z_t f_n(k_t, n_t), \ k_t = \frac{\varepsilon - 1}{\varepsilon} \cdot z_t f_k(k_t, n_t)$$

THE LABOR WEDGE

