## **CALIBRATING THE RBC MODEL**

# **FEBRUARY 2, 2012**

Introduction

## **STEADY STATE**

- ☐ Deterministic steady state the natural point of approximation
- ☐ Shut down all shocks and set exogenous variables at their means
- ☐ The idea: let economy run for many (infinite) periods
  - ☐ Time eventually "doesn't matter" any more
  - ☐ Drop all time indices

$$\begin{split} -\frac{u_n(\overline{c},\overline{n})}{u_c(\overline{c},\overline{n})} &= \overline{z} F_n(\overline{k},\overline{n}) \\ u_c(\overline{c},\overline{n}) &= \beta u_c(\overline{c},\overline{n}) \Big[ \overline{z} F_k(\overline{k},\overline{n}) + 1 - \delta \Big] \\ \overline{c} &+ \delta \overline{k} &= \overline{z} F(\overline{k},\overline{n}) \end{split}$$

 $\ln \overline{z} = (1 - \rho_z) \ln \overline{z} + \rho_z \ln \overline{z} \Rightarrow \overline{z} = \overline{z}$  (a parameter of the model)

- $\hfill\Box$  Given functional forms and parameter values, solve for  $(\overline{c},\overline{n},\overline{k})$ 
  - ☐ The steady state of the model
  - ☐ Taylor expansion around this point

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Introduction

#### **CALIBRATION - PHILOSOPHY**

- ☐ An economic model is a measuring device
- ☐ If model makes "believable" predictions along some important dimensions (i.e., "matches some key data")...
- $\hfill\Box$  ...then maybe its predictions are "believable" along the novel dimensions of the model
- ☐ Getting some "partial derivatives" of the model in known directions correct...
- $\hfill\Box$  ...may build credibility that its "partial derivatives" in novel directions are at least not grossly incorrect

February 2, 2012

3

Introduction

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- $\hfill\Box$  ...then maybe its predictions are "believable" along the novel dimensions of the model
- Getting some "partial derivatives" of the model in known directions correct...
- ...may build credibility that its "partial derivatives" in novel directions are at least not grossly incorrect
- Make model match some data of interest often long-run (i.e., time-averaged data) growth facts
  - □ Preferably well-accepted "stylized facts"
  - ☐ Solow growth model in the background
  - Natural candidate: Kaldor growth facts
- □ Calibration vs. Estimation

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Introduction

#### CALIBRATION OF BASELINE RBC MODEL

- ☐ Must take a stand on three (related) points
  - ☐ Which data do we want model to match? (even constructing data is challenging...)
  - ☐ Functional forms (utility, production)
  - ☐ Parameter values
- ☐ Choose functional forms consistent with "Kaldor-plus facts"
  - (K1) Capital income share and labor income share of GDP are stationary
  - (K2) All real quantity variables grow at same rate in the long run
  - ☐ (K3) Real interest rate is stationary
  - (K4) Hours per worker are stationary
  - (K5) (K2) requires trend productivity to be labor-augmenting (Phelps 1966)

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5

Introduction

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- $\hfill \Box$
- But "true" calibration begins with model featuring <u>only</u> long-run growth
  - Puts restrictions on instantaneous utility and production forms
  - □ Use (K1)-(K5) to obtain these restrictions
- □ Richer models: more calibration targets and/or treating data differently
  - ☐ Monopoly markups (e.g., Dixit-Stiglitz and sticky price models)
  - Probability of finding a job (e.g., labor search models)
  - $\begin{tabular}{ll} \Box & Durable consumption vs. non-durable consumption \\ \end{tabular}$

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#### Calibration of RBC Model with Growth

## **RBC Model with Growth**

- ☐ Absent shocks, TFP grows at deterministic rate y
- □ Planner problem/perfect competition

 $\max E_0 \sum_{t=0}^{\infty} b^t u(C_t, n_t) \qquad \text{subject to}$   $C_t + K_{t+1} - (1 - \delta)K_t = z_t F(K_t, n_t X_t)$ 

Trend productivity is laboraugmenting (Harrod-neutral) (Makes use of fact (K5))

Red indicates variables or parameters that will be modified when detrending the model

 $X_{t} = \gamma X_{t-1}, \qquad \gamma \ge 1$ 

Flow resource constraint

Evolution of deterministic component of productivity

given stochastic process for evolution of  $z_t$  and  $(K_0, z_0, X_0)$ 

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7

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Flow resource constraint

Red indicates variables or parameters that will be modified when detrending the model  $\begin{aligned} \boldsymbol{C}_{t} + \boldsymbol{K}_{t+1} - (1 - \delta) \boldsymbol{K}_{t} &= \boldsymbol{z}_{t} F(\boldsymbol{K}_{t}, \boldsymbol{n}_{t} \boldsymbol{X}_{t}) \\ \boldsymbol{X}_{t} &= \gamma \boldsymbol{X}_{t-1}, \qquad \gamma \geq 1 \end{aligned}$ 

Evolution of deterministic component of productivity

given stochastic process for evolution of  $\boldsymbol{z}_t$  and  $(\boldsymbol{K}_0,\,\boldsymbol{z}_0,\,\boldsymbol{X}_0)$ 

- □ Suppose  $z_t = 1$  always, so only deterministic growth
- Deterministic dynamics of  $(C_t, K_{t+1}, n_t, X_{t+1})$  governed by

(1)  $-\frac{u_n(C_t, n_t)}{u_c(C_t, n_t)} = X_t F_2(K_t, n_t X_t)$ 

Labor supply function (aka consumption-labor optimality)

(2)  $\frac{u_C(C_t, n_t)}{bu_C(C_{t+1}, n_{t+1})} = F_1(K_{t+1}, n_{t+1}X_{t+1}) + 1 - \delta$ 

Capital supply function (aka consumption-savings optimality)

(3)  $C_t + K_{t+1} - (1 - \delta)K_t = F(K_t, n_t X_t)$ 

 $X_{t} = \gamma X_{t-1}$ 

Normalize  $X_0 = 1$ 

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## **RESTRICTIONS ON FUNCTIONAL FORMS**

- Deterministic dynamics of  $(C_t, K_{t+1}, n_t, X_t)$  governed by
- $-\frac{u_n(C_t, n_t)}{u_c(C_t, n_t)} = X_t F_2(K_t, n_t X_t)$  (3)  $C_t + K_{t+1} (1 \delta)K_t = F(K_t, n_t X_t)$ 
  - $\frac{u_{C}(C_{t}, n_{t})}{bu_{C}(C_{t+1}, n_{t+1})} = F_{1}(K_{t+1}, n_{t+1}X_{t+1}) + 1 \delta$  (4)  $X_{t} = \gamma X_{t-1}$ (2)
- (K1) Capital income share and labor income share of GDP are stationary And viewing economic profits as zero

$$\Rightarrow F(K, nX) = K^{\alpha} (nX)^{1-\alpha} \quad (\alpha \approx 0.4)$$

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Calibration of RBC Model with Growth

## **RESTRICTIONS ON FUNCTIONAL FORMS**

- Deterministic dynamics of ( $C_{t'}$   $K_{t+1'}$   $n_{t_r}$   $X_t$ ) governed by
  - $-\frac{u_{n}(C_{i}, n_{i})}{u_{c}(C_{i}, n_{i})} = (1 \alpha)X_{i} \left(\frac{K_{i} / X_{i}}{n_{i}}\right)^{a}$   $\frac{u_{c}(C_{i}, n_{i})}{bu_{c}(C_{i+1}, n_{i+1})} = \alpha \left(\frac{K_{i+1} / X_{i+1}}{n_{i+1}}\right)^{a-1} + 1 \delta$ (4)  $X_{i} = \gamma X_{i-1}$ (1)

## **RESTRICTIONS ON FUNCTIONAL FORMS**

Deterministic dynamics of  $(C_t, K_{t+1}, n_t, X_t)$  governed by

$$-\frac{u_n(C_t, n_t)}{u_c(C_t, n_t)} = (1 - \alpha) X_t \left( \frac{K_t / X_t}{n_t} \right)^{\alpha}$$

(3) 
$$C_t + K_{t+1} - (1 - \delta)K_t = K_t^{\alpha} (n_t X_t)^{1-\alpha}$$

(2) 
$$\frac{u_C(C_t, n_t)}{bu_1(C_t, n_t)} = \alpha \left( \frac{K_{t+1}/X_{t+1}}{n_t} \right)^{\alpha-1} + 1 - \delta$$

$$-\frac{u_{n}(C_{t}, n_{t})}{u_{c}(C_{t}, n_{t})} = (1 - \alpha) X_{t} \left(\frac{K_{t} / X_{t}}{n_{t}}\right)^{\alpha}$$

$$\frac{u_{c}(C_{t}, n_{t})}{bu_{c}(C_{t+1}, n_{t+1})} = \alpha \left(\frac{K_{t+1} / X_{t+1}}{n_{t+1}}\right)^{\alpha - 1} + 1 - \delta$$
(4)
$$X_{t} = \gamma X_{t-1}$$

(K2) All real quantity variables grow at same rate in the long run

$$\Rightarrow \frac{Y_{t+1}}{Y_t} = \frac{C_{t+1}}{C_t} = \frac{K_{t+1}}{K_t} = \frac{X_{t+1}}{X_t} = \gamma, \quad \forall t$$

$$\Rightarrow y_t \equiv \frac{Y_t}{X_t} = \overline{y}, \quad k_t \equiv \frac{K_t}{X_t} = \overline{k}, \quad c_t \equiv \frac{C_t}{X_t} = \overline{c}, \quad \forall t$$

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Calibration of RBC Model with Growth

## **RESTRICTIONS ON FUNCTIONAL FORMS**

Deterministic dynamics of  $(C_{t'}, K_{t+1'}, n_{t_t}, X_t)$  governed by

(1) 
$$-\frac{u_n(C_i, n_i)}{u_c(C_i, n_i)} = (1 - \alpha) X_i \left( \frac{K_i / X_i}{n_i} \right)^{\alpha}$$
(3) 
$$C_i + K_{i+1} - (1 - \delta) K_i = K_i^{\alpha} (n_i X_i)^{1 - \alpha}$$
(2) 
$$\frac{u_C(C_i, n_i)}{b u_C(C_{i+1}, n_{i+1})} = \alpha \left( \frac{K_{i+1} / X_{i+1}}{n_{i+1}} \right)^{\alpha - 1} + 1 - \delta$$
(4) 
$$X_i = \gamma X_{i-1}$$

(3) 
$$C_t + K_{t+1} - (1-\delta)K_t = K_t^{\alpha}(n_t X_t)^{1-\delta}$$

(2) 
$$\frac{u_C(C_i, n_i)}{bu_C(C_{i+1}, n_{i+1})} = \alpha \left(\frac{K_{i+1} / X_{i+1}}{n_{i+1}}\right)^{\alpha - 1} + 1 - \delta$$

$$X_{t} = \gamma X_{t-1}$$

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$$\Rightarrow \frac{Y_{t+1}}{Y_t} = \frac{C_{t+1}}{C_t} = \frac{K_{t+1}}{K_t} = \frac{X_{t+1}}{X_t} = \gamma, \quad \forall t$$

$$Y_t = \frac{X_{t+1}}{X_t} = \frac{C_{t+1}}{X_t} = \frac{C_{t+1}$$

$$\Rightarrow y_{t} \equiv \frac{Y_{t}}{X_{t}} = \overline{y}, \quad k_{t} \equiv \frac{K_{t}}{X_{t}} = \overline{k}, \quad c_{t} \equiv \frac{C_{t}}{X_{t}} = \overline{c}, \quad \forall t$$

And scale (3) by 
$$X_t$$
 to make stationary
$$-\frac{u_n(C_t,n_t)}{u_c(C_t,n_t)} = (1-\alpha)X_t \left(\frac{k_t}{n_t}\right)^a$$
Note long run growth rate affects capital accumulation even in stationary representation!
$$c_t + \gamma k_{t+1} - (1-\delta)k_t = k_t^a n_t^{1-\alpha}$$

$$k_{t+1} - (1 - \delta)k_t = k_t^a n_t^{1 - a}$$

$$\frac{u_{C}(C_{t}, n_{t})}{bu_{C}(C_{t+1}, n_{t+1})} = \alpha \left(\frac{k_{t+1}}{n_{t+1}}\right)^{\alpha - 1} + 1 - \delta$$

$$X_t = \gamma X_{t-1}$$

## **RESTRICTIONS ON FUNCTIONAL FORMS**

Deterministic dynamics of  $(C_t, n_t, X_t)$  governed by

$$-\frac{u_n(C_t, n_t)}{u_c(C_t, n_t)} = (1 - \alpha) X_t \left(\frac{\overline{k}}{n_t}\right)^{\alpha}$$

(3) 
$$\overline{c} + \gamma \overline{k} - (1 - \delta) \overline{k} = \overline{k}^{\alpha} n_{t}^{1 - \alpha}$$

(1) 
$$-\frac{u_n(C_t, n_t)}{u_c(C_t, n_t)} = (1 - \alpha) X_t \left(\frac{\overline{k}}{n_t}\right)^{\alpha}$$
(2) 
$$\frac{u_c(C_t, n_t)}{bu_c(C_{t+1}, n_{t+1})} = \alpha \left(\frac{\overline{k}}{n_{t+1}}\right)^{\alpha-1} + 1 - \delta$$

$$X_{t} = \gamma X_{t-1}$$

(K4) Hours per worker are stationary

$$\Rightarrow n_{t} = \overline{n}$$

along deterministic path. BUT  $\overline{n}$  is endogenous...

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Calibration of RBC Model with Growth

## **RESTRICTIONS ON FUNCTIONAL FORMS**

Deterministic dynamics of  $C_t$  governed by

(1) 
$$-\frac{u_n(C_t, \overline{n})}{u_c(C_t, \overline{n})} = (1 - \alpha)X_t \left(\frac{\overline{k}}{\overline{n}}\right)^{\alpha}$$

(3) 
$$\overline{c} + \gamma \overline{k} - (1 - \delta) \overline{k} = \overline{k}^{\alpha} \overline{n}^{1 - \alpha}$$

(2) 
$$\frac{u_C(C_i, \overline{n})}{bu_C(C_{i+1}, \overline{n})} = \alpha \left(\frac{\overline{k}}{\overline{n}}\right)^{\alpha-1} + 1 - \epsilon$$

- Implied already (RHS of (2)) is
  - (K3) Real interest rate is stationary
- Final step - functional form for utility?
- **Observations** 
  - Optimal choice of labor ( $\overline{n}$ ) must be independent of  $X_t$  (from (1))
    - Requires offsetting income and substitution effects of wages (long-run productivity) on labor supply
  - IMRS can only depend on  $C_{t+1}/C_t$  (from (2)), which in turn =  $\gamma$

#### Calibration of RBC Model with Growth

### **RESTRICTIONS ON FUNCTIONAL FORMS**

- Deterministic dynamics of  $C_t$  governed by
- $\overline{c} + \gamma \overline{k} (1 \delta) \overline{k} = \overline{k}^{\alpha} \overline{n}^{1 \alpha}$
- $-\frac{u_n(C_t, \overline{n})}{u_c(C_t, \overline{n})} = (1 \alpha)X_t \left(\frac{\overline{k}}{\overline{n}}\right)^{\alpha}$  $\frac{u_c(C_t, \overline{n})}{bu_c(C_{t+1}, \overline{n})} = \alpha \left(\frac{\overline{k}}{\overline{n}}\right)^{\alpha-1} + 1$ (2)
- Implied already (RHS of (2)) is
  - (K3) Real interest rate is stationary
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- **Observations** 
  - Optimal choice of labor ( $\overline{n}$ ) must be independent of  $X_t$  (from (1))
    - Requires offsetting income and substitution effects of wages (long-run productivity) on labor supply
  - IMRS can only depend on  $C_{t+1}/C_t$  (from (2)), which in turn =  $\gamma$
- Two requirements together imply

$$u(C_i,n_i) = \begin{cases} \left[\frac{C_i v(n_i)\right]^{1-\sigma}-1}{1-\sigma} & \text{if } \sigma > 0, \ \sigma \neq 1 \\ \ln C_i + v(n_i) & \text{if } \sigma = 1 \end{cases}$$
 King, Plosser, Rebelo (1988 *JME*)

February 2, 2012 15

RBC Model with Growth

## **STEADY STATE**

- Steady state  $(\overline{c}, \overline{n}, \overline{k})$  solves (1), (2), (3)
- A dynamic phenomenon!
  - Not static!
  - Economy is moving exactly along its long-run (i.e., deterministic) growth path
- Scale of absolute quantity outcomes within model is meaningless
  - What does, e.g.,  $\overline{c}$  = 1.56 mean?

RBC Model with Growth

## STEADY STATE

- Steady state  $(\overline{c}, \overline{n}, \overline{k})$  solves (1), (2), (3)
  - A dynamic phenomenon!
    - □ Not static!

- ☐ Economy is moving exactly along its long-run (i.e., deterministic) growth path
- □ Balanced growth path
- □ Scale of absolute quantity outcomes within model is meaningless
  - □ What does, e.g.,  $\overline{c} = 1.56$  mean?
- □ Relative quantity outcomes are interpretable
  - □ Provide calibration targets
  - e.g.,  $\overline{c}/\overline{y} = 0.70$ ,  $\overline{k}/\overline{y} = 2.5$  (if annual measurement)
- ☐ Time use and intertemporal price outcomes within model are interpretable
  - □ Provide calibration targets
  - $\overline{n}$  is fraction of time spent in paid market work
    - □ Empirical:  $n \approx 0.30$
- □ Use ss calibration targets to set parameter values, given functional forms

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Transformed RBC Model

## **RBC Model Without Growth**

□ Often start instead with

$$u(c_i, n_i) = \begin{cases} \left[c_i v(n_i)\right]^{1-\sigma} - 1 & \text{if } \sigma > 0, \ \sigma \neq 1 \\ 1 - \sigma & \text{if } \sigma > 1 \end{cases} \quad \text{and} \quad \sum_{t=0}^{\infty} \beta^t u(c_i, n_i)$$

$$c_t = c_t / X_t \quad \text{if } \sigma = 1$$

February 2, 2012 18

Transformed RBC Model

## **RBC Model Without Growth**

☐ Often start instead with

 $u(c_{i}, n_{i}) = \begin{cases} \frac{\left[c_{i}v(n_{i})\right]^{1-\sigma} - 1}{1 - \sigma} & \text{if } \sigma > 0, \ \sigma \neq 1 \\ \ln c_{i} + v(n_{i}) & \text{if } \sigma = 1 \end{cases} \quad \text{and} \quad \sum_{t=0}^{\infty} \beta^{t}u(c_{i}, n_{t})$ 

- $\Box$  For this transformed model to deliver same steady state (relative quantities, time use, and r), require

  - □ Subjective discount factor  $\beta \equiv b\gamma^{1-\sigma}$  (King and Rebelo, p. 945)
- □ Typical assumption y = 1 omits growth altogether
- □ What if trend growth rate fluctuates,  $\gamma_t$ ?
  - Typical representation cannot accommodate trend shocks because y = 1
  - □ Trend shocks fairly common in small-open-economy models
  - Affects discount factor and capital accumulation equation

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Calibration of RBC Model: Typical Approach

## **BASELINE RBC MODEL**

- □ Assuming  $\gamma = 1...$
- □ ...complete calibration?
- □ Data: long-run labor income share of GDP  $\approx$  0.60
  - $\square$  Cobb-Douglas F(.) implies

$$\frac{wn}{F(k,n)} = \frac{(1-\alpha)k^{\alpha}n^{1-\alpha}}{k^{\alpha}n^{1-\alpha}} = 1-\alpha \qquad \Rightarrow \qquad \alpha = 0.40$$

 $\square$  Data: long-run ratio of (annual) gross investment to capital stock  $\approx 0.07$ 

$$\frac{k - (1 - \delta)k}{k} = \frac{\delta k}{k} = 0.07$$
  $\Rightarrow$   $\delta = 0.07$  (annual) or 0.018 (quarterly)

February 2, 2012 20

### **BASELINE RBC MODEL**

- □ Assuming  $\gamma = 1...$
- □ ...complete calibration?
- **Data:** long-run labor income share of GDP  $\approx 0.60$ 
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$$\frac{k - (1 - \delta)k}{k} = \frac{\delta k}{k} = 0.07$$
  $\Rightarrow$   $\delta = 0.07$  (annual) or 0.018 (quarterly)

- Data: long-run ratio of (annual) output to capital stock  $\approx 0.4$
- ☐ Steady-state Euler equation

$$1 = \beta \left[ \frac{\alpha k^{\alpha} n^{1-\alpha}}{k} + 1 - \delta \right] = \beta \left[ \frac{\alpha F(k, n)}{k} + 1 - \delta \right] \implies \beta = 0.95 \text{ (annual) or } 0.99 \text{ (quarterly)}$$

OR Data: avg. net real return on capital  $\approx$  5% per year (e.g, return on S&P500)

Steady-state Euler equation

$$f_k(k,n) = \frac{1}{\beta} - 1 + \delta$$
  $\Rightarrow$   $\beta = 0.96$  (annual) or 0.99 (quarterly)

February 2, 2012 21

Calibration of RBC Model: Typical Approach

### **BASELINE RBC MODEL**

☐ Utility parameters

$$u(c_i,n_i) = \begin{cases} \frac{\left[c_i v(n_i)\right]^{1-\sigma} - 1}{1-\sigma} & \text{if } \sigma > 0, \ \sigma \neq 1\\ \ln c_i + v(n_i) & \text{if } \sigma = 1 \end{cases}$$

- □ Data: IES is around unity(?) or lower
  - □ Implies  $\sigma > 1$

  - $\sigma = 1$  a conventional value
- □ Labor subutility
  - □ Common form

$$v(n) = -\frac{\psi}{1 + 1/\eta} n^{1 + 1/\eta}$$

- π measures Frisch elasticity of labor supply (use C-L optimality condition)
- $\Box \qquad \text{Calibrate } \pmb{\varPsi} \text{ to hit } \ \overline{n} \approx 0.3$
- ☐ Empirical evidence on Frisch elasticity?

February 2, 2012 22

#### Calibration of RBC Model: Typical Approach

### **BASELINE RBC MODEL**

- ☐ Labor supply elasticity "controversial"
- Micro evidence: very low  $\eta$  (substantially) smaller than one
- **■** Macro evidence: very high  $\eta$  (substantially) larger than one
- □ "Tension" between macro and micro evidence not useful way to frame the "controversy"
- ☐ Micro studies pick up intensive margin of labor supply
- ☐ Macro studies pick up (mostly) extensive margin of labor supply
  - ☐ And other frictions in allocation of workers to jobs...
- Chetty (2010): uses both macro and micro evidence to put bounds on labor supply elasticity
- □ Common in DSGE models:  $\eta > 1$

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Calibration of RBC Model: Typical Approach

### **BASELINE RBC MODEL**

☐ Exogenous process for TFP (deviations from long-run trend productivity)

$$\ln z_{t+1} = (1 - \rho_z) \ln \overline{z} + \rho_z \ln z_t + \varepsilon_{t+1}$$

$$\varepsilon_{t+1} \sim \text{iid } N(0, \sigma_z^2)$$

- $\square$  Normalize  $\overline{z} = 1$ 
  - Only governs absolute scale of model, which is arbitrary
  - $\Box$  What does, e.g.,  $\overline{c}$  =1.56 mean?
- $\square$  Construct time-series for  $z_t$  using
  - □ Data on labor, (detrended) capital, and (detrended) output
- ☐ AR(1) estimation
  - □ Quarterly frequency

 $\Rightarrow \rho_z = 0.95$  and  $\sigma_z = 0.006$ 

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Summary

# USING THE RBC (OR ANY DSGE) MODEL

- 1. Dream up/construct/write fully-articulated model
  - ☐ Ideally to answer questions motivated by data and with hypotheses
- 2. Choose parameter values
  - Perhaps extremely rigorously, if goal is to match certain empirical facts very precisely
  - Perhaps adopting generally-accepted values, if goal is to illustrate some insight
- 3. Solve for deterministic steady state (balanced growth path)
- Solve for dynamic decision rules (e.g., linear approximation, second-order approximation, global approximation)
- 5. Conduct informative battery of experiments (impulse responses, simulations, etc.) to try to falsify hypotheses
- 6. Tabulate results, write a (good!) paper, get it published