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# **OPTIMAL MONETARY POLICY**

**FEBRUARY 15, 2017**

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# OPTIMAL POLICY PROBLEMS: GENERAL FORM

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- ❑ Set up economic environment

- ❑ Household problem

- ❑ Firm problem

- ❑ Specification of government policy

- ❑ Policy tools (monetary, fiscal, or both monetary and fiscal)

KEY ISSUE:

Lump-sum tax available or not?



- ❑ Government budget constraint(s)

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- ❑ Solve for/define private-sector equilibrium

- ❑ **For any arbitrary policy**

- ❑ Define social welfare criterion

- ❑ Representative-consumer model: expected discounted lifetime utility

- ❑ Heterogeneous-consumer model: not as obvious...how to weight?

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- ❑ Choose (typically state-contingent) policy rules **subject to all equilibrium conditions of economy**

- ❑ Optimal policy-maker is a Social Planner with the additional restrictions imposed by decentralized equilibrium

# FISCAL OR NOT?

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- ❑ **New Keynesian optimal-policy models**
  - ❑ Typical claim: “abstracting from fiscal issues” ...
  - ❑ **...but monetary policy usefully thought of as a type of fiscal policy**
    - ❑ **Affects relative prices!**
      - ❑ i.e., affects slopes of budget constraints – how different from fiscal policy?
  - ❑ (Soon...) Typical NK optimal-policy model allows sufficiently-rich set of (lump-sum and proportional) fiscal instruments to make decentralized economy Pareto-efficient
    - ❑ A very strong statement regarding fiscal policy
    - ❑ How does this **abstract** from fiscal policy?...

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    - A very strong statement regarding fiscal policy
    - How does this **abstract** from fiscal policy?...
  
- **Ramsey optimal-policy models**
  - Explicitly consider fiscal issues – either in isolation or in conjunction (jointly) with monetary policy
  - **Strength:** fully-specified stand on macroeconomic policy
  - **Weakness:** is the stand ad-hoc? (criticism by the recent “New Dynamic Public Finance” literature...see, e.g., Werning (2007 *QJE*))

# OPTIMAL MONETARY POLICY: A FIRST LOOK

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- Main focus: how do sticky nominal prices affect the optimal conduct of monetary policy?
  - In environment with explicit optimization by households and firms

# OPTIMAL MONETARY POLICY: A FIRST LOOK

- ❑ Main focus: how do sticky nominal prices affect the optimal conduct of monetary policy?
    - ❑ In environment with explicit optimization by households and firms
  - ❑ Sticky nominal prices
    - ❑ Model using Taylor staggering (two-period staggering)
    - ❑ (And typical Dixit-Stiglitz monopoly model underneath)
  - ❑ No money demand
    - ❑ i.e., no CIA, MIU, etc.
    - ❑ Append a quantity equation ( $P_t c_t = M_t$ ) to make model “monetary”
      - ❑ NOT a CIA constraint (i.e., appended AFTER household optimization)
  - ❑ Lump-sum taxes/transfers finance monetary policy ( $M_{t+1} = M_t + T_t$ )
  - ❑ Adopt the **primal formulation**
  - ❑ Assume **commitment**
  - ❑ Assume **timeless perspective**
- } General issues to be aware of/take a stand on for any optimal policy analysis



# GENERAL ISSUES

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- ❑ **Primal Formulation**
  - ❑ Formulate optimal policy problem **in terms of only allocations**
    - ❑ By eliminating policy variables (and prices) using equilibrium conditions
  - ❑ Given optimal allocation, construct (implied) policy instruments that support allocation
    - ❑ Ramsey (1927)
    - ❑ **Approach often employed in fiscal policy models**
    - ❑ Only recently applied more frequently to monetary policy models

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## □ Commitment

- With initial state variable and/or forward-looking equilibrium conditions, policy FOCs for  $t = 0$  **differ** from policy FOCs for  $t > 0$
- Assume government can bind itself to state-contingent policy paths for  $t > 0$
- (Opposite of commitment is **discretion**)

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Lucas and Stokey (1983), Chari, Christiano, and Kehoe (1991)

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Interpretation: the optimal policy has *already* been in operation for a long time; ignoring transition dynamics associated with initially-suboptimal policies

## □ Timeless Perspective

- Set  $t = 0$  state to the steady-state of the  $t > 0$  policy FOCs



# OPTIMAL MONETARY POLICY: A FIRST LOOK

- Key constraint on optimal policy is the (sticky-price firm's) optimal price-setting condition – derived from two-period Taylor pricing problem

Instantaneous profit depends on price, output, and mc

$$p_{0,t} \cdot \frac{\partial pr(p_{0,t}, y_{0,t}, mc_t)}{p_{0,t}} + E_t \left\{ \Xi_{t+1|t} p_{1,t+1} \cdot \frac{\partial pr(p_{1,t+1}, y_{1,t+1}, mc_{t+1})}{p_{1,t+1}} \right\} = 0$$

Optimal *relative* price set by sticky-price firm

*Discount factor* between  $t$  and  $t+1$  because *dynamic* firm problem; in equilibrium, = household stochastic discount factor

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With two-period stickiness,  
 $p_{1,t+1} = p_{0,t} / \pi_{t+1}$

Recall: Inflation erodes a sticky-price firm’s relative price

$$p_{0,t} \cdot \frac{\partial pr(p_{0,t}, y_{0,t}, mc_t)}{p_{0,t}} + E_t \left\{ \Xi_{t+1|t} \cdot p_{1,t+1} \cdot \frac{\partial pr(p_{1,t+1}, y_{1,t+1}, mc_{t+1})}{p_{1,t+1}} \right\} = 0$$

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Optimal relative price set by sticky-price firm

Discount factor between  $t$  and  $t+1$  because dynamic firm problem; in equilibrium, = household stochastic discount factor

Use demand function to substitute out  $p_{i,s}$

$$x(y_{0,t}, y_t, n_t, z_t) + E_t \left\{ \Xi_{t+1|t} x(y_{1,t+1}, y_{t+1}, n_{t+1}, z_{t+1}) \right\} = 0$$

Constraint for primal representation

Type-0 firm output

Final output labor

Aggregate

Aggregate TFP

Type-1 firm output

Firm "type" simply is number of periods since the most recent nominal price adjustment

# OPTIMAL MONETARY POLICY: A FIRST LOOK

## □ Optimal Policy Problem

$$\max_{\{y_{0,t}, y_{1,t}, y_t, c_t, n_{0,t}, n_{1,t}, n_t\}} E_0 \left[ \sum_{t=0}^{\infty} \beta^t u(c_t, n_t) \right] \text{ subject to sequences}$$

$$c_t = y_t$$

$$n_t = \frac{1}{2} n_{0,t} + \frac{1}{2} n_{1,t}$$

$$y_{0,t} = z_t n_{0,t}$$

$$y_{1,t} = z_t n_{1,t}$$

$$y_t = \left[ 0.5 \cdot y_{0,t}^{(\varepsilon-1)/\varepsilon} + 0.5 \cdot y_{1,t}^{(\varepsilon-1)/\varepsilon} \right]^{\varepsilon/(\varepsilon-1)}$$

$$x(y_{0,t}, y_t, n_t, z_t) + E_t \left\{ \Xi_{t+1|t} x(y_{1,t+1}, y_{t+1}, n_{t+1}, z_{t+1}) \right\} = 0$$

Final goods market clearing  
(consumption the only source of absorption)

Labor-market clearing  
(each firm "type" has measure 1/2)

Production functions symmetric  
across the two "types" of firms

Dixit-Stiglitz final-goods aggregator

Optimal price-setting condition  
(of firms that re-adjust price)



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**IMPORTANT:** Optimization w.r.t. period- $t$  choices requires differentiating through period- $(t-1)$  optimal price-setting condition if assuming commitment!

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This term disappears if flexible prices

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multiplier

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$$\omega_t \quad n_t = \frac{1}{2} n_{0,t} + \frac{1}{2} n_{1,t}$$

Labor-market clearing  
(each firm "type" has measure 1/2)

$$\rho_{1t} \quad y_{0,t} = z_t n_{0,t}$$

$$\rho_{2t} \quad y_{1,t} = z_t n_{1,t}$$

} Production functions symmetric across the two "types" of firms

$$\lambda_t \quad y_t = \left[ 0.5 \cdot y_{0,t}^{(\varepsilon-1)/\varepsilon} + 0.5 \cdot y_{1,t}^{(\varepsilon-1)/\varepsilon} \right]^{\varepsilon/(\varepsilon-1)}$$

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Dixit-Stiglitz final-goods aggregator

$$\rightarrow x(y_{0,t}, y_t, n_t, z_t) + E_t \left\{ \Xi_{t+1|t} x(y_{1,t+1}, y_{t+1}, n_{t+1}, z_{t+1}) \right\} = 0$$

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- Key constraint on optimal policy is the (sticky-price firm's) optimal price-setting condition – derived from two-period Taylor pricing problem

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- FOC on  $n_t$  (to illustrate commitment problem)

$$u_n(c_t, n_t) + \phi_t \frac{\partial x(y_{0,t}, y_t, n_t, z_t)}{\partial n_t} + \frac{1}{\beta} \phi_{t-1} E_{t-1} \left\{ \Xi_{t|t-1} \frac{\partial x(y_{1,t}, y_t, n_t, z_t)}{\partial n_t} \right\} = \omega_t$$

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multiplier

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Note  $t-1$  subscripts!

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- Time  $t-1$  decisions (hence equilibrium) based on  $t-1$  information set
  - Including expectation of period- $t$  policy
  - Source of time-inconsistency problems in policy models with forward-looking equilibrium conditions
    - Kydland and Prescott (1977)

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- Importance of  $\Phi_{t-1}$ 
  - From perspective of period- $t$  policy optimization: **measures the gain to period- $t-1$  price-setters of a period- $t$  policy**
  - From perspective of computing the optimal-policy equilibrium of economy: **a state variable**



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  - From perspective of computing the optimal-policy equilibrium of economy: **a state variable**
  - In period  $t$ , “temptation” exists for policy-maker to “forget about” period  $t-1$  – **i.e., can implement a one-shot Pareto-superior equilibrium in period  $t$  by “supposing  $\Phi_{t-1} = 0$ ”**
    - Basic idea of Kydland and Prescott (1977) example
  - General: optimal policy problems with commitment and forward-looking equilibrium conditions feature **lagged Lagrange multipliers**

See King and Wolman (1999, p. 384)

## OPTIMAL MONETARY POLICY: RESULTS

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- Policy FOCs imply  $y_{0,t} = y_{1,t}$  for all  $t$  (assuming  $\Phi_{-1} = \Phi_{\text{infinity}}$ )
  - **Output should be equated across firms adjusting price and firms not adjusting price**
    - Follows from symmetry and concavity of Dixit-Stiglitz aggregator
    - Achieves Pareto optimum
  - In equilibrium, can only be achieved if relative price across types of goods = 1

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- In equilibrium, can only be achieved if relative price across types of goods = 1
- **In monetary economy with sticky nominal price-setting, requires zero inflation at all dates and in all states**
  - Induce an allocation in which when firms DO have an opportunity to reset nominal price, they optimally choose to NOT change price at all
  - Completely eliminates any deadweight loss stemming from nominal rigidities (dispersion in Calvo and Taylor models, direct resource cost in Rotemberg model)

## LOW AND STABLE INFLATION

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- ❑ **Zero inflation** the benchmark optimal policy in **sticky-price models**
  - ❑ In the long run (steady state)...
  - ❑ ...and in the short run (business-cycle magnitude shocks)
  
- ❑ **Small (Friedman Rule) deflation** the benchmark optimal policy in **flexible-price models with money demand distortions**
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- ❑ **Sticky-price + money demand distortions**
  - ❑ Long-run optimal policy: deflation **between** zero and the Friedman Rule
    - ❑ Khan, King, and Wolman (2003 *ReStud*)
    - ❑ Schmitt-Grohe and Uribe (2004 *JET*)
    - ❑ Siu (2004 *JME*)
  - ❑ Short-run optimal policy: **small** inflation fluctuations in all dates/states
    - ❑ Same references...

# IMPLEMENTATION OF OPTIMAL POLICY?

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- ❑ King and Wolman use primal approach
  - ❑ Allows for characterizing optimal policy (optimal allocations) without describing how policy should be implemented
  - ❑ Primal approach largely silent on implementation
  
- ❑ **Implementation:** how **should/can**  $X$  percent inflation be achieved?
  - ❑ Long-run: set  $X$  percent money growth (monetarist)
  - ❑ Short-run: ?...

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  - ❑ Short-run: ?...
  
- ❑ Typical New Keynesian optimal-policy analysis
  - ❑ Assume a simple Taylor Rule as the operational rule by which policy is implemented
 
$$\hat{R}_t = \delta_\pi \hat{\pi}_t + \delta_y \hat{y}_t$$
  - ❑ Characterize constrained-optimal allocations
  - ❑ Find coefficients of Taylor Rule that deliver allocations very close to the constrained-optimal allocations