
OPTIMAL FISCAL POLICY WITH LABOR SELECTION

APRIL 20, 2017

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ **Labor market structure and analysis changing over the years**
 - ❑ **Secular changes**
 - ❑ **Cyclical changes**
- ❑ **Labor market conditions a prime concern for policy**
- ❑ **Search and matching in labor markets**
- ❑ **Technological primitives**
 - ❑ **Costs of posting job openings**
 - ❑ **Matching function**
- ❑ **But many other components of hiring costs**

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ **Labor market structure and analysis changing over the years**
 - ❑ **Secular changes**
 - ❑ **Cyclical changes**
- ❑ **Labor market conditions a prime concern for policy**
- ❑ **Search and matching in labor markets**
- ❑ **Technological primitives**
 - ❑ **Costs of posting job openings**
 - ❑ **Matching function**
- ❑ **But many other components of hiring costs**
- ❑ **Screening/selection in labor markets**
- ❑ **Technological primitives**
 - ❑ **Costs of integrating new workers into production process**
 - ❑ **Distribution of idiosyncratic “match-quality” shocks for new workers**
- ❑ **(Davis, Faberman, & Haltiwanger (2013 QJE): \approx 60% of hiring costs are vacancy costs)**

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ Benevolent policy desires efficient labor markets
- ❑ **Characterization of efficient allocations (“first-best”)**
 - ❑ **Model-consistent efficiency**
 - ❑ **Model-consistent distortions**
- ❑ **Builds on analysis of**
 - ❑ **GE selection efficiency in Chugh and Merkl (2015 *IER*)**
 - ❑ **GE matching efficiency in Arseneau and Chugh (2012 *JPE*)**

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ Benevolent policy desires efficient labor markets
- ❑ **Characterization of efficient allocations (“first-best”)**
 - ❑ Model-consistent efficiency
 - ❑ Model-consistent distortions
- ❑ Builds on analysis of
 - ❑ GE selection efficiency in Chugh and Merkl (2015 *IER*)
 - ❑ GE matching efficiency in Arseneau and Chugh (2012 *JPE*)
- ❑ **Characterization of optimal policy**
 - ❑ Ramsey (1927) (“second-best”)
 - ❑ Lucas and Stokey (1984 *JME*), CCK (1991 *JMCB*, 1999 *Handbook of Macro*), Werning (2007 *QJE*), many others
 - ❑ Recent summary by Stiglitz (2014 *NBER WP*)
- ❑ **Pigovian corrective taxation**
 - ❑ Ramsey (1927) was response to question posed by Pigou **w/o** lump-sum T
 - ❑ Pigou (1928, *A Study in Public Finance*) incorporated Ramsey results **w/** T

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ Calibrate exogenous policy economy to hit empirical volatility of
 - ❑ ue , lfp , and $\eta(\varepsilon)$
- ❑ Requires distortionary structural parameters
- ❑ Conduct optimal policy given structural parameters

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ Calibrate exogenous policy economy to hit empirical volatility of
 - ❑ ue , lfp , and $\eta(\varepsilon)$
- ❑ Requires distortionary structural parameters
- ❑ Conduct optimal policy given structural parameters
- ❑ Labor tax rate smoothing not optimal in either selection model...

	Labor Selection		Walrasian
Relative SD (wrt GDP)	1.0		≈ 0 (CCK 1999, Werning 2007 QJE, many others)

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ Calibrate exogenous policy economy to hit empirical volatility of
 - ❑ ue , lfp , and $\eta(\varepsilon)$
- ❑ Requires distortionary structural parameters
- ❑ Conduct optimal policy given structural parameters
- ❑ Labor tax rate smoothing not optimal in either selection model...
- ❑ ...or in matching model

	Labor Selection	Labor Matching	Walrasian
Relative SD (wrt GDP)	1.0	5.6 (Arseneau and Chugh 2012 JPE)	≈ 0 (CCK 1999, Werning 2007 QJE, many others)

LABOR MARKETS – STRUCTURE AND POLICY

- ❑ Calibrate exogenous policy economy to hit empirical volatility of
 - ❑ ue , lfp , and $\eta(\epsilon)$
- ❑ Requires distortionary structural parameters
- ❑ Conduct optimal policy given structural parameters
- ❑ Labor tax rate smoothing not optimal in either selection model...
- ❑ ...or in matching model

	Labor Selection	Labor Matching	Walrasian
Relative SD (wrt GDP)	1.0	5.6 <small>(Arseneau and Chugh 2012 JPE)</small>	≈ 0 <small>(CCK 1999, Werning 2007 QJE, many others)</small>

- ❑ Hiring subsidies large in long-run – $\tau^h = 81\%$
- ❑ Hiring subsidies volatile in business cycles
- ❑ **Economic difference vs. Walrasian labor markets?**

LABOR MARKETS – MODEL-CONSISTENT WEDGES

- ❑ **Technological primitives**

- ❑ **Develop selection-model consistent transformation function and MRTs**
 - ❑ **Aggregate goods resource constraint**
 - ❑ **Aggregate law of motion of employment**

- ⇒ model-consistent decentralized wedges**

- ❑ **Tax volatility ⇒ EFFICIENT fluctuations**
 - ❑ **Selection model wedge fluctuations EXACTLY = 0**

LABOR MARKETS – MODEL-CONSISTENT WEDGES

- ❑ **Technological primitives**
- ❑ **Develop selection-model consistent transformation function and MRTs**
 - ❑ **Aggregate goods resource constraint**
 - ❑ **Aggregate law of motion of employment**

⇒ **model-consistent decentralized wedges**
- ❑ **Tax volatility ⇒ EFFICIENT fluctuations**
 - ❑ **Selection model wedge fluctuations EXACTLY = 0**
- ❑ **Analytically characterize source of externalities**
 - ❑ **Cost gap = marginal hiring cost – avg. hiring cost**
- ❑ **“Selection Market Tightness”**
 - ❑ **Play highly similar role as market tightness externalities in matching model**
- ❑ **Compare and contrast with search and matching model**

CONTRIBUTION TO LABOR & POLICY LITERATURES

- ❑ **Need to know appropriate “wedges” for designing optimal policy**
 - ❑ **Fiscal policy**
 - ❑ **Monetary policy**
 - ❑ **Regulatory policy**

- ❑ **Recent literature on labor selection**
 - ❑ **Lechthaler, Merkl, and Snower (2010 *JECD*)**
 - ❑ **Merkl and van Rens (2012)**
 - ❑ **Brown, Merkl, and Snower (2015 *MD*)**
 - ❑ **Faia, Lechthaler, and Merkl (2014 *JMCB*) (optimal monetary policy)**
 - ❑ **Baydur (2017 *AEJ: Macro*) – partial match quality revelation**

- ❑ **Previous work**
 - ❑ **Arseneau, Chahrour, Chugh, Finkelstein Shapiro (2015 *JMCB*) (customer matching)**
 - ❑ **Chugh and Ghironi (2015) (endogenous product varieties)**
 - ❑ **Arseneau and Chugh (2012 *JPE*)**
 - ❑ **Aruoba and Chugh (2010 *JET*) (new monetarist)**
 - ❑ **Arseneau and Chugh (2008 *JME*) (nominal wage rigidities in labor matching model)**

OUTLINE

- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (**labor search and matching** + **labor selection**)
 - ❑ Focus on **labor selection** model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ **Conclusion**

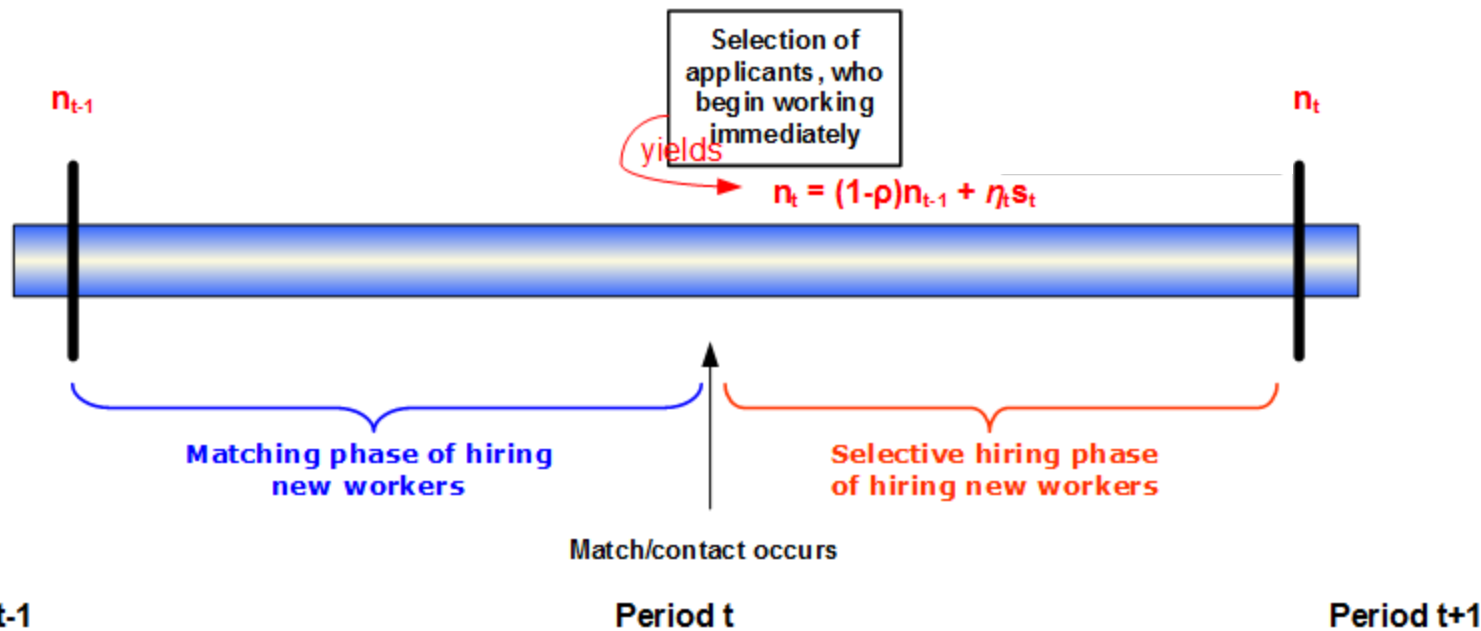
OUTLINE

- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ **Conclusion**

LABOR MARKET STRUCTURE

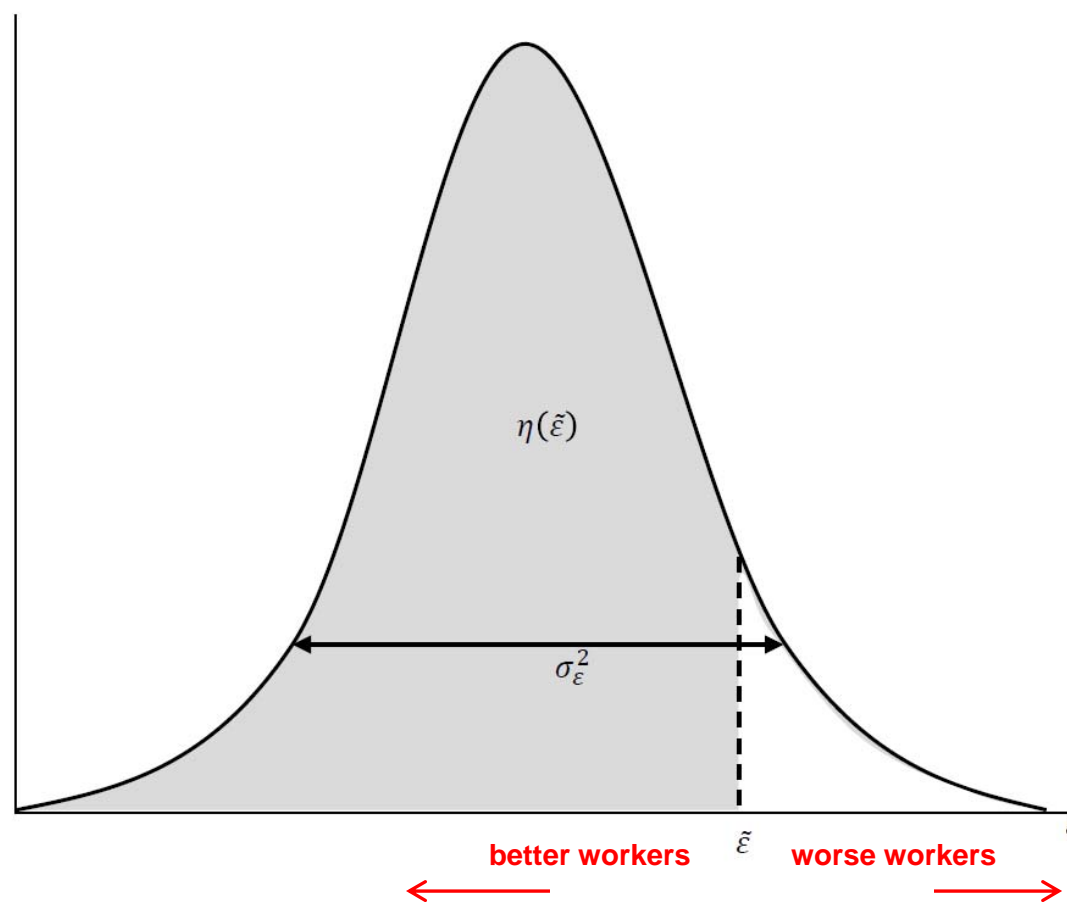
- Matching and **selection** two distinct concepts of frictional labor markets

↑
"match quality"



LABOR MARKET STRUCTURE

- Distribution of idiosyncratic hiring costs ε_i



LABOR MARKET STRUCTURE

- $\tilde{\varepsilon}_t$ endogenous selection threshold
- $\eta(\tilde{\varepsilon}_t)$ endogenous selection probability
- $\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$ average training cost for all newly-selected employees
- σ_ε cross-sectional SD of training cost distribution
- v_t vacancies
- k_t^h matching probability for actively searching individual
- γ vacancy posting cost
- $m(s_t, v_t)$ aggregate matching function

OUTLINE

- ❑ Model – Structure of Labor Markets
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ Positive analysis (non-Ramsey policy)
- ❑ Ramsey equilibrium
- ❑ Calibration
- ❑ Normative analysis (Ramsey policy) – wedge/distortion smoothing
- ❑ Compare and contrast with search and matching model
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ Conclusion

MATCHING + SELECTION EFFICIENCY

□ **Social Planner**

$$\max_{\{c_t, n_t, s_t, \tilde{\epsilon}_t, v_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)]$$

$$lfp_t \equiv (1 - \eta(\tilde{\epsilon}_t)k_t^h)s_t + n_t$$

s.t.

$$c_t + g_t + \frac{H(\tilde{\epsilon}_t)}{\eta(\tilde{\epsilon}_t)} \cdot \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t) + \gamma v_t = z_t n_t$$

Goods resource constraint

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t)$$

Aggregate LOM for total employment

MATCHING + SELECTION EFFICIENCY

□ **Social Planner**

$$\max_{\{c_t, n_t, s_t, \tilde{\epsilon}_t, v_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)]$$

$lfp_t \equiv (1 - \eta(\tilde{\epsilon}_t)k_t^h)s_t + n_t$

s.t.

$$c_t + g_t + \frac{H(\tilde{\epsilon}_t)}{\eta(\tilde{\epsilon}_t)} \cdot \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t) + \gamma v_t = z_t n_t$$

Goods resource constraint

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t)$$

Aggregate LOM for total employment

Efficient LFP

$$\frac{h'(lfp_t)}{u'(c_t)} = m_s(s_t, v_t) \cdot [\tilde{\epsilon}_t \cdot \eta(\tilde{\epsilon}_t) - H(\tilde{\epsilon}_t)]$$

Efficient vacancy creation

$$\frac{\gamma}{m_v(s_t, v_t)} = \tilde{\epsilon}_t \cdot \eta(\tilde{\epsilon}_t) - H(\tilde{\epsilon}_t)$$

... rewrite in terms of model-consistent wedges ...

Intertemporal Efficiency

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1 - \rho) [\tilde{\epsilon}_{t+1} - m_s(s_{t+1}, v_{t+1}) (\tilde{\epsilon}_{t+1} \eta(\tilde{\epsilon}_{t+1}) - H(\tilde{\epsilon}_{t+1}))]}{\tilde{\epsilon}_t - z_t}$$

MATCHING + SELECTION EFFICIENCY

□ **Social Planner**

$$\max_{\{c_t, n_t, s_t, \tilde{\epsilon}_t, v_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)]$$

$$lfp_t \equiv (1 - \eta(\tilde{\epsilon}_t)k_t^h)s_t + n_t$$

s.t.

$$c_t + g_t + \frac{H(\tilde{\epsilon}_t)}{\eta(\tilde{\epsilon}_t)} \cdot \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t) + \gamma v_t = z_t n_t$$

Goods resource constraint

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t)$$

Aggregate LOM for total employment

Efficient LFP – identical to Arseneau and Chugh 2012 JPE (p. 949, eqn. 21)

$$\frac{h'(lfp_t)}{u'(c_t)} = \frac{\gamma \cdot m_s(s_t, v_t)}{m_v(s_t, v_t)}$$

MRT between non-participation and output

Intertemporal Efficiency

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1 - \rho) \left[\tilde{\epsilon}_{t+1} - m_s(s_{t+1}, v_{t+1}) (\tilde{\epsilon}_{t+1} \eta(\tilde{\epsilon}_{t+1}) - H(\tilde{\epsilon}_{t+1})) \right]}{\tilde{\epsilon}_t - z_t}$$

IMRT: quantity of c_{t+1} that can be produced by reducing c_t by one unit, all else equal, by accumulating “wealth” in form of employment

SELECTION EFFICIENCY

□ **Social Planner**

$$\max_{\{c_t, n_t, s_t, \tilde{\epsilon}_t, v_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)]$$

s.t.

$$c_t + g_t + \frac{H(\tilde{\epsilon}_t)}{\eta(\tilde{\epsilon}_t)} \cdot \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t) + \gamma v_t = z_t n_t$$

$$lfp_t \equiv (1 - \eta(\tilde{\epsilon}_t) k_t^h) s_t + n_t$$

Goods resource constraint

$$n_t = (1 - \rho) n_{t-1} + \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t)$$

Aggregate LOM for total employment

SELECTION EFFICIENCY

□ **Social Planner**

$$\max_{\{c_t, n_t, s_t, \tilde{\epsilon}_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)]$$

$$lfp_t \equiv (1 - \eta(\tilde{\epsilon}_t))s_t + n_t$$

s.t.

$$c_t + g_t + \frac{H(\tilde{\epsilon}_t)}{\eta(\tilde{\epsilon}_t)} \cdot \eta(\tilde{\epsilon}_t) \cdot s_t = z_t n_t$$

Goods resource constraint

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\epsilon}_t) \cdot s_t$$

Aggregate LOM for total employment

□ $\gamma = 0$

zero vacancy posting cost

□ $m(s_t, v_t) = s_t^\xi v_t^{1-\xi}$

trivial matching function

↓ if $\xi = 1$

$$m(s_t, v_t) = s_t$$

Crucial obs. #1 for decentralized efficiency

SELECTION EFFICIENCY

□ **Social Planner**

$$lfp_t \equiv (1 - \eta(\tilde{\varepsilon}_t))s_t + n_t$$

$$\max_{\{c_t, n_t, s_t, \tilde{\varepsilon}_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)]$$

s.t.

$$c_t + g_t + \frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} \cdot \eta(\tilde{\varepsilon}_t) \cdot s_t = z_t n_t$$

Goods resource constraint

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\varepsilon}_t) \cdot s_t$$

Aggregate LOM for total employment

Efficient LFP

$$\frac{h'(lfp_t)}{u'(c_t)} = \underbrace{\tilde{\varepsilon}_t \cdot \eta(\tilde{\varepsilon}_t) - H(\tilde{\varepsilon}_t)}$$

MRT between non-participation and output

Intertemporal Efficiency

Derivation in Appendix D based on transformation frontier

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1 - \rho) \left(\tilde{\varepsilon}_{t+1} - \left(\tilde{\varepsilon}_{t+1} \cdot \eta(\tilde{\varepsilon}_{t+1}) - H(\tilde{\varepsilon}_{t+1}) \right) \right)}{\tilde{\varepsilon}_t - z_t}$$

IMRT: quantity of c_{t+1} that can be produced by reducing c_t by one unit, all else equal, by accumulating "wealth" in form of employment

OUTLINE

- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ **Conclusion**

OVERVIEW

- ❑ **Infinitely-lived representative household, measure one of members**
 - ❑ **Full consumption insurance amongst**
 - ❑ **Employed members**
 - ❑ **Unemployed members**
 - ❑ **Members outside the labor force (“leisure”)**
 - ❑ **Labor income taxation**
 - ❑ **Government-provided hiring subsidies**
 - ❑ **Government-provided unemployment benefits**
 - ❑ **Individual-specific Nash bargaining for newly-hired worker with ε_i**
 - ❑ **Only an extensive labor margin, no intensive labor margin**
 - ❑ **Long-lasting labor-market relationships – exogenous separation rate ρ**
- } Guarantees completeness of tax instruments (Ramsey issue)

FIRMS

- **Production**
 - **New job i produces $y_{it} = z_t - \varepsilon_{it}$ (output – hiring cost)**
 - **Hiring costs subsidized at rate τ^h**
 - **(Each incumbent job produces $y_t = z_t$)**

	New hires	Avg. hiring costs	Avg. wage for new workers	Marg. wage for threshold new worker	Wage for incumbent worker	“Tightness”
	$n_t^{NEW} = \eta(\tilde{\varepsilon}_t) s_t$	$\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$	$\frac{\omega_e(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$	$w(\tilde{\varepsilon}_t)$	w_t^I	$\tilde{\varepsilon}_t \cdot \eta(\tilde{\varepsilon}_t) - H(\tilde{\varepsilon}_t)$

FIRMS

- **Production**
 - **New job i produces $y_{it} = z_t - \varepsilon_{it}$ (output – hiring cost)**
 - **Hiring costs subsidized at rate τ^h**
 - **(Each incumbent job produces $y_t = z_t$)**

	New hires	Avg. hiring costs	Avg. wage for new workers	Marg. wage for threshold new worker	Wage for incumbent worker	“Tightness”
	$n_t^{NEW} = \eta(\tilde{\varepsilon}_t) s_t$	$\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$	$\frac{\omega_e(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$	$w(\tilde{\varepsilon}_t)$	w_t^I	$\tilde{\varepsilon}_t \cdot \eta(\tilde{\varepsilon}_t) - H(\tilde{\varepsilon}_t)$

- **Selection condition (aka labor demand) condition**

$$(1 - \tau_t^h) \cdot \tilde{\varepsilon}_t = z_t - w(\tilde{\varepsilon}_t) + (1 - \rho) E_t \left\{ \Xi_{t+1} \left[(1 - \tau_{t+1}^h) \cdot \tilde{\varepsilon}_{t+1} + w(\tilde{\varepsilon}_{t+1}) - w_{t+1}^I \right] \right\}$$

Cost of hiring = expected payoff of hiring

- **Given individualistic wage setting, holds for every new worker**

$$(1 - \tau_t^h) \cdot \varepsilon_{it} = z_t - w(\varepsilon_{it}) + (1 - \rho) E_t \left\{ \Xi_{t+1} \left[(1 - \tau_{t+1}^h) \cdot \tilde{\varepsilon}_{t+1} + w(\tilde{\varepsilon}_{t+1}) - w_{t+1}^I \right] \right\}$$

HOUSEHOLD OPTIMIZATION

- Maximize expected lifetime utility

$$\max_{\{c, n_t, s_t, b_t\}} E_0 \sum_{t=0}^{\infty} \beta^t \left[u(c_t) - \underbrace{h((1-\eta_t)s_t + n_t)}_{\text{disutility of participation}} \right]$$

s.t.

$$c_t + \sum_j \frac{1}{R_t^j} b_{t+1}^j = \underbrace{(1-\rho)n_{t-1} \cdot (1-\tau_t^n)w_t^I}_{\text{wages for measure of incumbent employees}} + \underbrace{(1-\tau_t^n) \cdot \left(\frac{\omega_{et}}{\eta_t} \right) \cdot \eta_t \cdot s_t}_{\text{wages for measure of newly-hired employees}} + \underbrace{(1-\eta_t)s_t\chi + b_t}_{\text{ue benefits for unemployed}} + \underbrace{(1-\tau^{pr})\Pi_t}_{\text{aggregate flow dividends received lump sum}}$$

View χ as fixed institutional parameter, not a cyclical policy choice

HOUSEHOLD OPTIMIZATION

- Maximize expected lifetime utility

$$\max_{\{c_t, n_t, s_t, b_t\}} E_0 \sum_{t=0}^{\infty} \beta^t \left[u(c_t) - h((1-\eta_t)s_t + n_t) \right]$$

disutility of participation

aggregate flow dividends received lump sum

s.t.

$$c_t + \sum_j \frac{1}{R_t^j} b_{t+1}^j = \underbrace{(1-\rho)n_{t-1} \cdot (1-\tau_t^n)w_t^I}_{\text{wages for measure of incumbent employees}} + \underbrace{(1-\tau_t^n) \cdot \left(\frac{\omega_{et}}{\eta_t} \right) \cdot \eta_t \cdot s_t}_{\text{wages for measure of newly-hired employees}} + \underbrace{(1-\eta_t)s_t\chi + b_t + (1-\tau^{pr})\Pi_t}_{\text{ue benefits for unemployed}}$$

View χ as fixed institutional parameter, not a cyclical policy choice

$$n_t = \underbrace{(1-\rho)n_{t-1}}_{\text{(exogenous) measure of pre-existing employment relationships terminate}} + \underbrace{\eta_t s_t}_{\text{flow of new employment relationships = measure of searchers } s_t \times \text{probability a searcher successfully lands a job}}$$

Perceived LOM for employment ("instantaneous production")

(exogenous) measure of pre-existing employment relationships terminate flow of new employment relationships = measure of searchers s_t x probability a searcher successfully lands a job

FOCs

HOUSEHOLD OPTIMIZATION

- **Optimal labor force participation (aka labor supply) condition**

$$\frac{h'(lfp_t)}{u'(c_t)} = \eta_t \left[(1 - \tau_t^n) \left(\frac{\omega_{et}}{\eta_t} \right) + (1 - \rho) E_t \left\{ \Xi_{t+1|t} \left[(1 - \tau_{t+1}^n) w_{t+1}^I + \frac{\mu_{ht+1}}{u'(c_{t+1})} \right] \right\} \right] + (1 - \eta_t) \chi$$

Envelope condition of period
t+1 hh-level problem
↓

- **Equates MRS cost with expected payoff of participation**

$$\begin{array}{c} \downarrow \\ \rho = 1 \\ \downarrow \\ \chi = 1 \\ \downarrow \\ \eta = 1 \end{array}$$

$$\frac{h'(lfp_t)}{u'(c_t)} = (1 - \tau_t^n) \omega_{et}$$

Nests RBC labor supply function

WAGES

- **Surplus sharing** via individualistic Nash bargaining power
 - Newly-hired employee bargaining power = α^E
 - Incumbent employee bargaining power = α^I

WAGES

□ **Surplus sharing** via individualistic Nash bargaining power

- Newly-hired employee bargaining power = α^E
- Incumbent employee bargaining power = α^I

$$w(\tilde{\varepsilon}_t) = \frac{\chi}{1 - \tau_t^n} + \text{PDV}_t$$

Wage for marginal
new worker

$$w(\varepsilon_{it}) = \frac{\chi}{1 - \tau_t^n} + \alpha^E (1 - \tau_t^h)(\tilde{\varepsilon}_t - \varepsilon_{it}) + \text{PDV}_t$$

Wage for infra-
marginal new
worker ε_{it}

WAGES

□ Surplus sharing via individualistic Nash bargaining power

- Newly-hired employee bargaining power = α^E
- Incumbent employee bargaining power = α^I

$$w(\tilde{\varepsilon}_t) = \frac{\chi}{1 - \tau_t^n} + \text{PDV}_t$$

Wage for marginal new worker

$$w(\varepsilon_{it}) = \frac{\chi}{1 - \tau_t^n} + \alpha^E (1 - \tau_t^h) (\tilde{\varepsilon}_t - \varepsilon_{it}) + \text{PDV}_t$$

Wage for infra-marginal new worker ε_{it}

$$\frac{\omega_e(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} = \frac{\chi}{1 - \tau_t^n} + \alpha^E (1 - \tau_t^h) \underbrace{\left(\tilde{\varepsilon}_t - \frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} \right)}_{\text{"Tightness"}} + \text{PDV}_t$$

Conditional average wage for all new workers

$$w_t^I = \frac{\chi}{1 - \tau_t^n} + \alpha^I (1 - \tau_t^h) \tilde{\varepsilon}_t + \text{PDV}_t$$

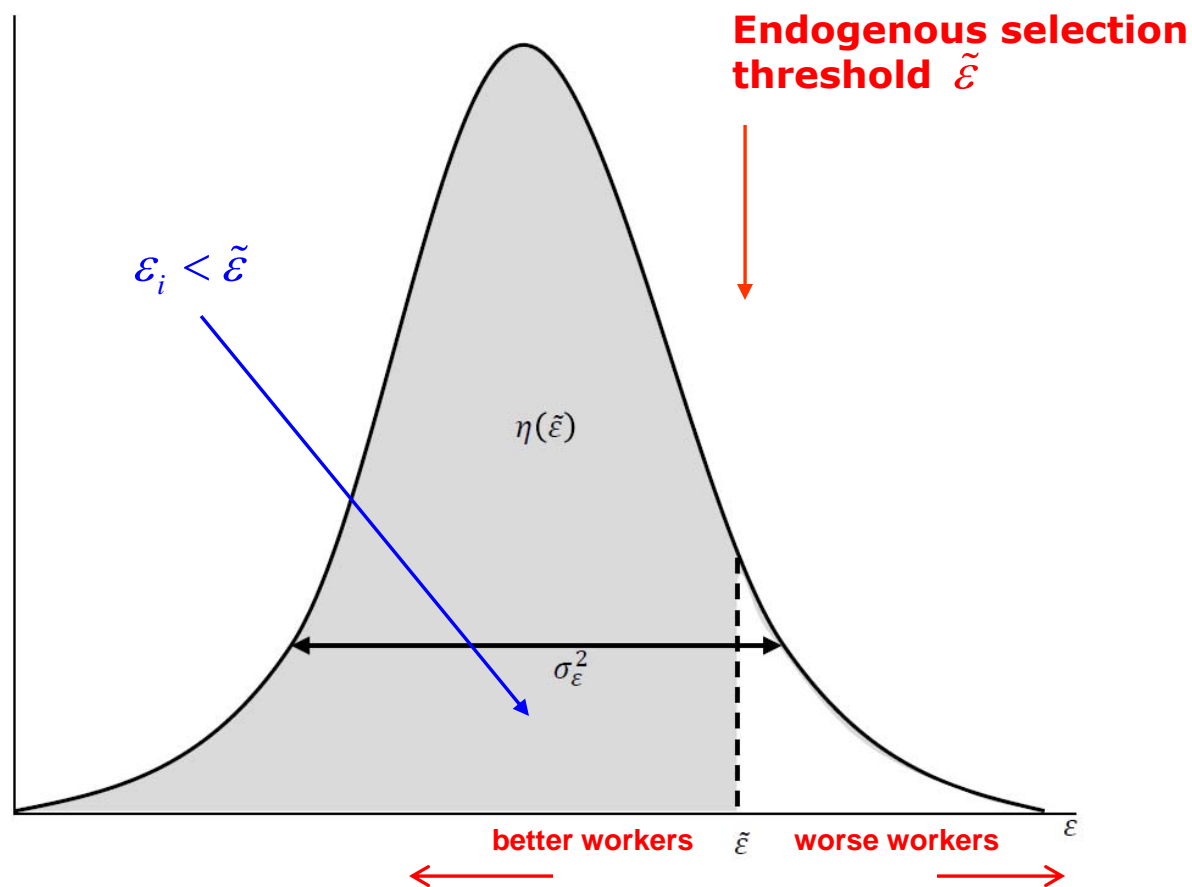
Wage for incumbent worker

□ Endogenous wage dispersion

- Within newly-hired employees
- Across newly-hired employees and incumbent employees

WAGES

- Distribution of idiosyncratic hiring costs ε_i



GOVERNMENT AND RESOURCE FRONTIER

- **Government**
 - **Government spending**
 - **Labor income tax**
 - **Hiring subsidies**
 - **Provision of ue benefits**
 - **One-period state contingent real debt**

- **Aggregate goods resource constraint**

$$c_t + g_t + \left(\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} \right) \eta(\tilde{\varepsilon}_t) s_t = z_t n_t$$

- **Aggregate LOM for labor**

$$n_t = (1 - \rho) n_{t-1} + \eta(\tilde{\varepsilon}_t) s_t$$

PRIVATE-SECTOR EQUILIBRIUM

- **State-contingent stochastic processes** $\{c_t, n_t, s_t, \tilde{\varepsilon}_t, w_t^l, w(\tilde{\varepsilon}_t), \omega_e(\tilde{\varepsilon}), R_t^j\}_{t=0}^{\infty}$ that satisfy
 - **Household's bond Euler equations**
 - **LFP condition**
 - **Selective hiring condition**
 - **Nash wage outcomes**
 - **Law of motion for employment** $n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\varepsilon}_t)s_t$
 - **Government budget constraint (key condition in Ramsey models)**
 - **Goods resource constraint** $c_t + g_t + \left(\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}\right)\eta(\tilde{\varepsilon}_t)s_t = z_t n_t$
 - **Given processes** $\{g_t, z_t, \tau_t^n, \tau_t^h\}_{t=0}^{\infty}$

OUTLINE

- ❑ Model – Structure of Labor Markets
- ❑ GE efficiency – definitions of model-consistent wedges
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ Ramsey equilibrium
- ❑ Calibration
- ❑ Normative analysis (Ramsey policy) – wedge/distortion smoothing
- ❑ Compare and contrast with search and matching model
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ Conclusion

OUTLINE

- ❑ Model – Structure of Labor Markets
- ❑ GE efficiency – definitions of model-consistent wedges
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ Positive analysis (non-Ramsey policy)
- ❑ **Ramsey equilibrium – optimize on $\tau^n(\mathbf{X}_t)$, $\tau^h(\mathbf{X}_t)$**
- ❑ Calibration
- ❑ Normative analysis (Ramsey policy) – wedge/distortion smoothing
- ❑ Compare and contrast with search and matching model
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ Conclusion

\mathbf{X}_t is private-sector decision functions

OUTLINE

- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium – optimize on $\tau^n(\mathbf{X}_t)$, $\tau^h(\mathbf{X}_t)$**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ **Conclusion**

\mathbf{X}_t is private-sector decision functions

CALIBRATION

- ❑ Parameterize so non-Ramsey economy generates empirically reasonable labor market fluctuations in ue , lfp , and hiring rate $\eta(\varepsilon)$
- ❑ Conditional on exogenous fluctuations in
 - ❑ Labor tax rate
 - ❑ Productivity
 - ❑ Government purchases
- ❑ **Crucial parameters – Part I**
 - ❑ **Distributional form** – logistic (also have used normal distribution)
 - ❑ Mean $\mu_\varepsilon = 0.30$
 - ❑ **Cross-sectional standard deviation $\sigma_\varepsilon = 0.19$**
- ❑ **Value of σ_ε disciplined by micro-level evidence**
 - ❑ **SD σ_ε across new hires of training costs = 207 hours (= 40% of MPN)**
 - ❑ Barron, Black, and Loewenstein (1989 *JLE*)
 - ❑ Firm-level costs of interviewing/hiring/training new workers
 - ❑ Based on 1982 EOPP (Employment Opportunities Pilot Project)

CALIBRATION

- ❑ Parameterize so non-Ramsey economy generates empirically reasonable labor market fluctuations in ue , lfp , and hiring rate $\eta(\varepsilon)$
- ❑ Conditional on exogenous fluctuations in
 - ❑ Labor tax rate
 - ❑ Productivity
 - ❑ Government purchases
- ❑ **Crucial parameters – Part I**
 - ❑ **Distributional form** – logistic (also have used normal distribution)
 - ❑ Mean $\mu_\varepsilon = 0.30$
 - ❑ **Cross-sectional standard deviation $\sigma_\varepsilon = 0.19$**
- ❑ **Crucial parameters – Part II**
 - ❑ Unemployment benefits = 0.70
 - ❑ Worker Nash bargaining power $\alpha^E = \alpha^I = 0.50$
 - ❑ For both new hires and incumbents
- ❑ Other parameters “standard” (Table 3)

Crucial obs. #2 for
decentralized efficiency

DYNAMIC RESULTS

			Non-Ramsey Policy (positive)	Data
Labor Tax Rate	Mean		20%	20%
	Rel. SD		0.98	1.8
“Tightness” ($\varepsilon\eta(\varepsilon) - H(\varepsilon)$)	Rel. SD		5.58	
Hiring rate $\eta(\varepsilon)$	Rel. SD		3.5	3.7
Unemployment	Rel. SD		8.6	5.2
LFP	Rel. SD		0.22	0.20

OUTLINE

- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium – optimize on $\tau^n(\mathbf{X}_t)$, $\tau^h(\mathbf{X}_t)$**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ **Conclusion**

\mathbf{X}_t is private-sector decision functions

DYNAMIC RESULTS

		Ramsey	Non-Ramsey Policy (positive)	Data
Labor Tax Rate	Mean	22%	20%	20%
	Rel. SD	0.98	0.98	1.8
"Tightness" ($\varepsilon\eta(\varepsilon) - H(\varepsilon)$)	Rel. SD	1.09	5.58	
Hiring rate $\eta(\varepsilon)$	Rel. SD	0.03	3.5	3.7
Unemployment	Rel. SD	5.3	8.6	5.2
LFP	Rel. SD	0.23	0.22	0.20

- Ramsey simulations: shocks to z, g conditional on structural parameters
- Observations
 1. Labor income tax rate smoothing **NOT** optimal
 2. Volatility of $\eta(\varepsilon)$ **much** smaller than in data

DYNAMIC RESULTS

		Ramsey Policy		
		Baseline parameters		Social Planner
Labor Tax Rate	Mean	22%		0%
	Rel. SD	0.99		0
"Tightness" ($\varepsilon\eta(\varepsilon) - H(\varepsilon)$)	Rel. SD	1.09		1.09
Hiring rate $\eta(\varepsilon)$	Rel. SD	0.03		0.03
Unemployment	Rel. SD	5.39		5.39
LFP	Rel. SD	0.04		0.04

- ❑ Social Planner simulations: shocks to z
- ❑ Ramsey simulations: Inefficient structural parameters DO appear in problem
- ❑ **Efficient surplus sharing**

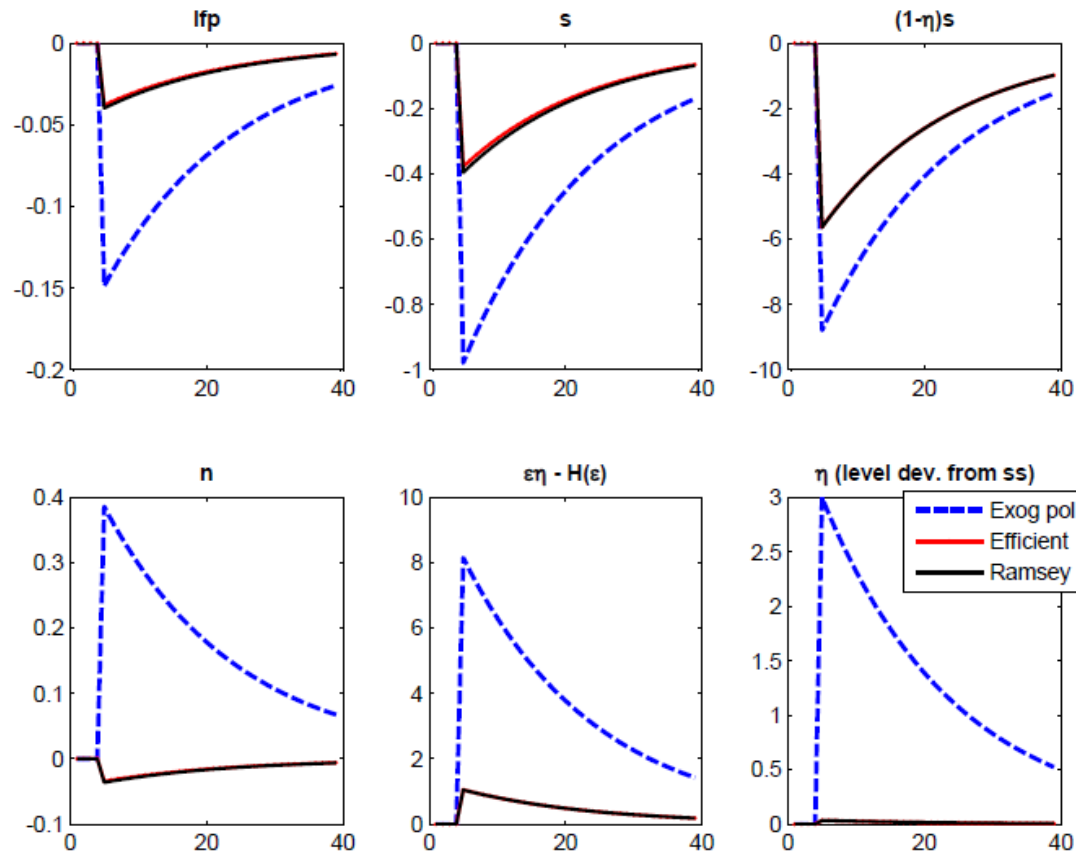
DYNAMIC RESULTS

		Ramsey Policy		
		Baseline parameters	For ANY (α, χ) pair	Social Planner
Labor Tax Rate	Mean	22%	---	0%
	Rel. SD	0.99	---	0
"Tightness" ($\varepsilon\eta(\varepsilon) - H(\varepsilon)$)	Rel. SD	1.09	1.09	1.09
Hiring rate $\eta(\varepsilon)$	Rel. SD	0.03	0.04	0.03
Unemployment	Rel. SD	5.39	5.39	5.39
LFP	Rel. SD	0.04	0.04	0.04

- ❑ Social Planner simulations: shocks to z
- ❑ Ramsey simulations: Inefficient structural parameters DO appear in problem
- ❑ Efficient surplus sharing for ANY (α, χ) pair

DYNAMIC RESULTS

□ Impulse response to productivity



OUTLINE

- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium – optimize on $\tau^n(\mathbf{X}_t)$, $\tau^h(\mathbf{X}_t)$**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
 - ❑ **Implications for Beveridge Curve**
 - ❑ Wage determination
 - ❑ Model-consistent wedges and “market tightness”
- ❑ **Conclusion**

\mathbf{X}_t is private-sector decision functions

BEVERIDGE CURVE

- ❑ **Outwards shift of Beveridge Curve during Great Recession**
 - ❑ **Elsby, Michaels, and Ratner (2015 *JEL*)**
 - ❑ **Diamond and Sahin (2014 *NY Fed Staff Report*)**

- ❑ **Reduced-form interpretation: “matching efficiency” Ω has declined**

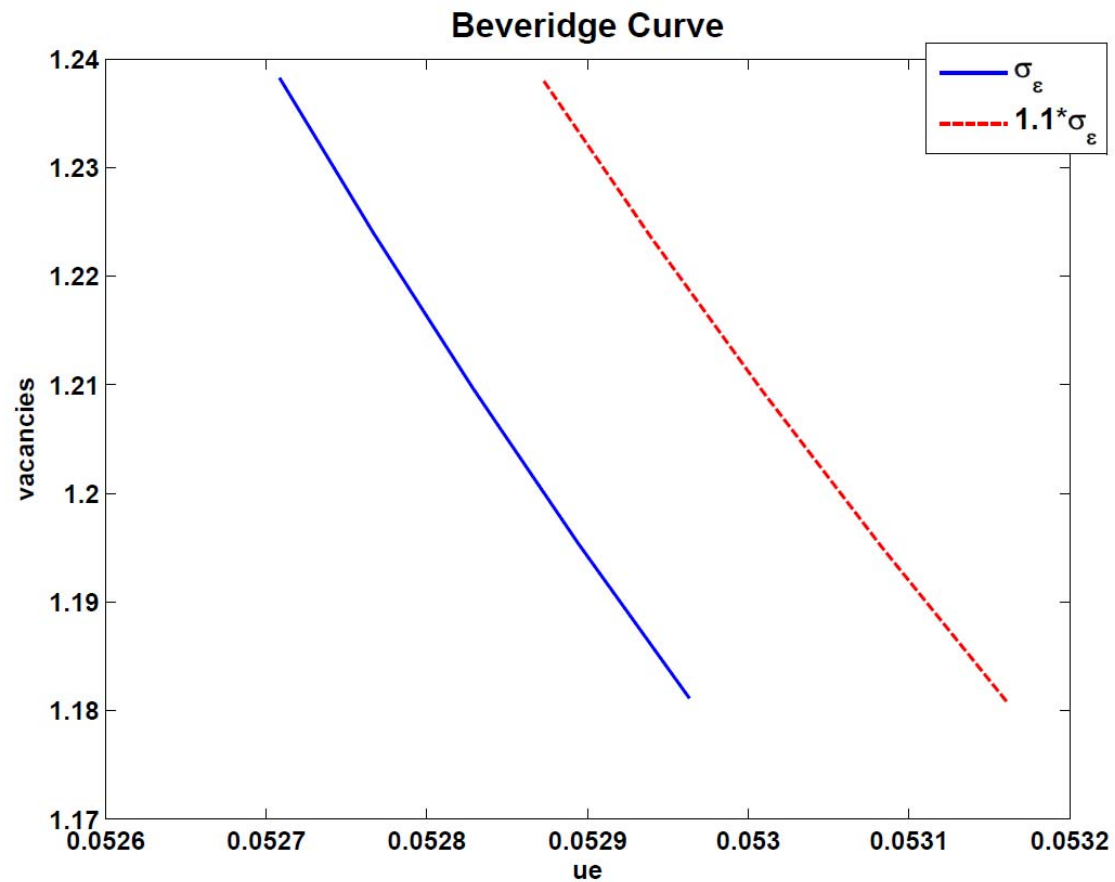
$$\Omega \cdot m(s_t, v_t)$$

- ❑ **Cheremukhin and Restrepo-Echavarria (2014 *EER*)**
 - ❑ **Pescatori and Tasci (2011)**
 - ❑ **Chahrour, Chugh, and Potter (2016)**

- ❑ **Proposal: increase in primitive cross-sectional SD σ_ε**
 - ❑ **Gets inside black-box Ω**
 - ❑ **(Distributional explanation at heart of Lester (2010 *JET*))**

BEVERIDGE CURVE

- **Outwards shift of Beveridge Curve during Great Recession**



OUTLINE

- ❑ Model – Structure of Labor Markets
- ❑ GE efficiency – definitions of model-consistent wedges
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ Positive analysis (non-Ramsey policy) \mathbf{X}_t is private-sector decision functions
- ❑ Ramsey equilibrium – optimize on $\tau^n(\mathbf{X}_t)$, $\tau^h(\mathbf{X}_t)$
- ❑ Calibration
- ❑ Normative analysis (Ramsey policy) – wedge/distortion smoothing
- ❑ **Compare and contrast with search and matching model**
 - ❑ Implications for Beveridge Curve
 - ❑ **Wage determination**
 - ❑ Model-consistent wedges and “market tightness”
- ❑ Conclusion

NASH BARGAINING & EFFICIENCY

- Suppose zero taxes in decentralized economy

- **Selection model (no search and matching)**

- (Trivial matching function)

$$\begin{aligned} m(s_t, v_t) &= s_t^\xi v_t^{1-\xi} && \text{(with } \xi = 1) \\ &= s_t \end{aligned}$$

- **Nash bargaining parameter $\alpha^E = \xi = 1$ achieves efficient allocations**

- **Efficient surplus sharing**

NASH BARGAINING & EFFICIENCY

- Suppose zero taxes in decentralized economy

- **Selection model (no search and matching)**

- **(Trivial matching function)**

$$m(s_t, v_t) = s_t^\xi v_t^{1-\xi} \quad (\text{with } \xi = 1)$$

$$= s_t$$

- **Nash bargaining parameter $\alpha^E = \xi = 1$ achieves efficient allocations**

- **Efficient surplus sharing**

- **Search and matching model (no selection)**

- **Matching function (fundamental)**

$$m(s_t, v_t) = s_t^\xi v_t^{1-\xi} \quad \xi \in (0.3, 0.7)$$

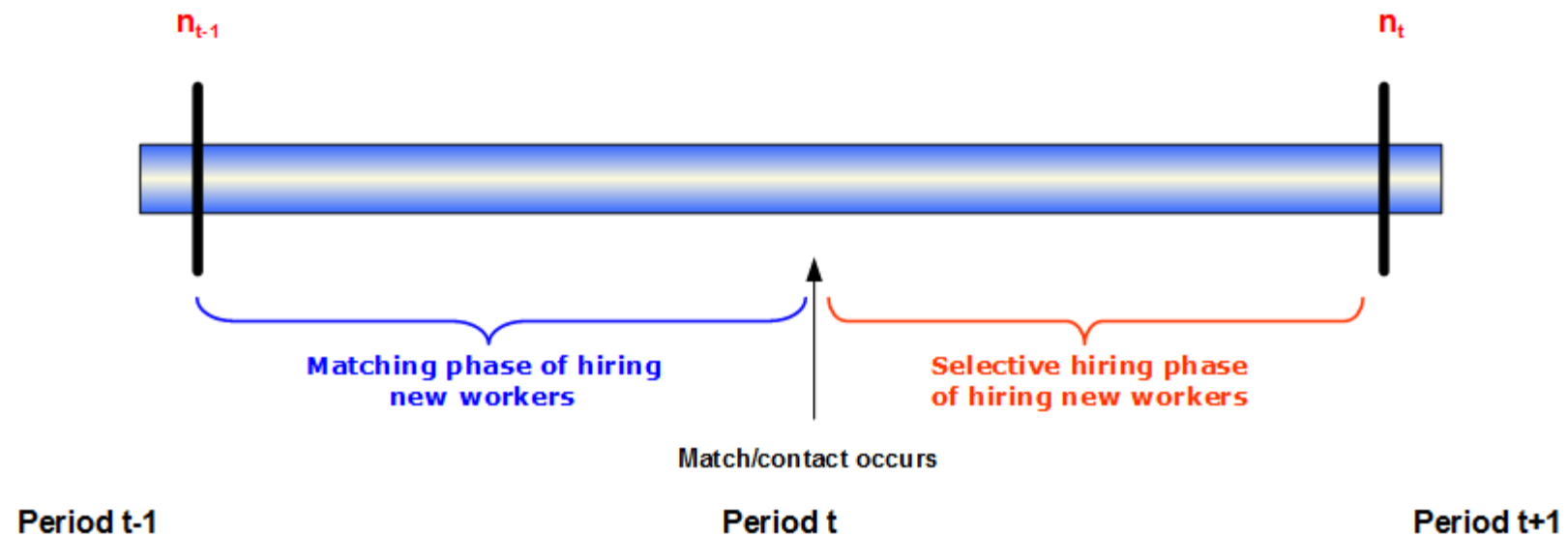
- **Nash bargaining parameter $\alpha^E = \xi < 1$ achieves efficient allocations**

- **Hosios (1990) condition**

- **Efficient surplus sharing**

NASH BARGAINING & EFFICIENCY

- ❑ Suppose zero taxes in decentralized economy
- ❑ **Matching** + **Selection**
- ❑ No value of α^E can decentralize efficient surplus sharing
 - ❑ Two competing efficiency goals...
 - ❑ ...but only ONE wage determination mechanism



OUTLINE

- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
 - ❑ Extended model (labor search and matching + labor selection)
 - ❑ Focus on labor selection model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium – optimize on $\tau^n(\mathbf{X}_t)$, $\tau^h(\mathbf{X}_t)$**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
 - ❑ Implications for Beveridge Curve
 - ❑ Wage determination
 - ❑ **Model-consistent wedges and “market tightness”**
- ❑ **Conclusion**

\mathbf{X}_t is private-sector decision functions

LABOR MARKETS – MODEL-CONSISTENT WEDGES

- Develop selection-model consistent transformation function and MRTs
 - Aggregate goods resource constraint
 - Aggregate law of motion of employment

⇒ model-consistent decentralized wedges

- Tax volatility ⇒ EFFICIENT fluctuations
 - Selection model wedge fluctuations EXACTLY = 0
- Analytically characterize source of externalities
 - Cost gap = marginal hiring cost – avg. hiring cost
- “Selection Market Tightness”
 - Play highly similar role as market tightness externalities in matching model

Efficient labor supply in matching model (Arseneau and Chugh 2012 JPE)

$$MRS_{c_t, n_t} = \gamma \cdot \left(\frac{\alpha}{1 - \alpha} \right) \cdot \theta_t$$

$$MRS_{c_t, n_t} = \tilde{\varepsilon}_t \cdot \eta(\tilde{\varepsilon}_t) - H(\tilde{\varepsilon}_t)$$

Efficient labor supply from Chugh and Merkl 2015 IER

LABOR MARKETS

Efficient labor supply in matching model (Arseneau and Chugh 2012 JPE)

$$\frac{h'(lfp_t)}{u'(c_t)} = \underbrace{\gamma \cdot \left(\frac{\alpha}{1-\alpha} \right) \cdot \theta_t}_{\text{Within-period MRT}}$$

Within-period MRT

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left(\frac{\gamma}{(1-\alpha)\theta_{t+1}^{-\alpha}} - \gamma \cdot \frac{\alpha}{1-\alpha} \cdot \theta_{t+1} \right)}{\underbrace{\frac{\gamma}{(1-\alpha)\theta_t^{-\alpha}} - z_t}_{\text{Intertemporal MRT}}}$$

Intertemporal MRT

LABOR MARKETS

Efficient labor supply in matching model (Arseneau and Chugh 2012 *JPE*)

$$\frac{h'(lfp_t)}{u'(c_t)} = \underbrace{\gamma \cdot \left(\frac{\alpha}{1-\alpha} \right) \cdot \theta_t}_{\text{Within-period MRT}}$$

Within-period MRT

$$\frac{h'(lfp_t)}{u'(c_t)} = \underbrace{\tilde{\epsilon}_t \cdot \eta(\tilde{\epsilon}_t) - H(\tilde{\epsilon}_t)}_{\text{Within-period MRT}}$$

Within-period MRT

Efficient labor supply in selection model (Chugh and Merkl 2015 *IER*)

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left(\frac{\gamma}{(1-\alpha)\theta_{t+1}^{-\alpha}} - \gamma \cdot \frac{\alpha}{1-\alpha} \cdot \theta_{t+1} \right)}{\frac{\gamma}{(1-\alpha)\theta_t^{-\alpha}} - z_t}$$

Intertemporal MRT

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left(\tilde{\epsilon}_{t+1} - (\tilde{\epsilon}_{t+1} \eta(\tilde{\epsilon}_{t+1}) - H(\tilde{\epsilon}_{t+1})) \right)}{\tilde{\epsilon}_t - z_t}$$

Intertemporal MRT



Substitute intratemporal conditions into intertemporal conditions

LABOR MARKETS

Marginal cost of hiring a new employee



$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left(\frac{\gamma}{(1-\alpha)\theta_{t+1}^{-\alpha}} - \frac{h'(lfp_{t+1})}{u'(c_{t+1})} \right)}{\frac{\gamma}{(1-\alpha)\theta_t^{-\alpha}} - z_t}$$

Marginal cost of hiring a new employee



$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left(\tilde{\epsilon}_{t+1} - \frac{h'(lfp_{t+1})}{u'(c_{t+1})} \right)}{\tilde{\epsilon}_t - z_t}$$

CONCLUSIONS

- ❑ **Selective hiring framework realistic**
- ❑ **Selective hiring costs are distinct from vacancy posting costs**
 - ❑ **Davis, Faberman, and Haltiwanger (2013 QJE): $\approx 40\%$ of hiring costs are NOT vacancy posting costs**
- ❑ **Smoothing (model-consistent) wedges the goal for optimal policy**
 - ❑ **Not smoothing policy instruments**
- ❑ **Model-consistent wedges apply to**
 - ❑ **Fiscal policy**
 - ❑ **Monetary policy**
 - ❑ **Regulatory policy**
- ❑ **Next step: analysis combining matching + selection**