



**OPTIMAL FISCAL POLICY WITH  
LABOR SELECTION**

**FEBRUARY 20, 2019**

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# LABOR MARKETS – STRUCTURE AND POLICY

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- ❑ **Labor market structure and analysis changing over the years**
  - ❑ **Secular changes**
  - ❑ **Cyclical changes**
- ❑ **Labor market conditions a prime concern for policy**
- ❑ **Search and matching in labor markets**
- ❑ **Technological primitives**
  - ❑ **Costs of posting job openings**
  - ❑ **Matching function**
- ❑ **But many other components of hiring costs**

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  - ❑ **Matching function**
- ❑ **But many other components of hiring costs**
- ❑ **Screening/selection in labor markets**
- ❑ **Technological primitives**
  - ❑ **Costs of integrating new workers into production process**
  - ❑ **Distribution of idiosyncratic “match-quality” shocks for new workers**
- ❑ **(Davis, Faberman, & Haltiwanger (2013 QJE):  $\approx$  60% of hiring costs are vacancy costs)**

# LABOR MARKETS – STRUCTURE AND POLICY

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- ❑ **Benevolent policy desires efficient labor markets**
- ❑ **Characterization of efficient allocations (“first-best”)**
  - ❑ **Model-consistent efficiency**
  - ❑ **Model-consistent distortions**
- ❑ **Builds on analysis of**
  - ❑ **GE selection efficiency in Chugh and Merkl (2016 *IER*)**
  - ❑ **GE matching efficiency in Arseneau and Chugh (2012 *JPE*)**

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- ❑ **Characterization of optimal policy**
  - ❑ Ramsey (1927) (“second-best”)
  - ❑ Lucas and Stokey (1984 *JME*), CCK (1991 *JMCB*, 1999 *Handbook of Macro*), Werning (2007 *QJE*), many others
  - ❑ Recent summary by Stiglitz (2014 *NBER WP*)
- ❑ **Pigovian corrective taxation**
  - ❑ Ramsey (1927) was response to question posed by Pigou **w/o** lump-sum  $T$
  - ❑ Pigou (1928, *A Study in Public Finance*) incorporated Ramsey results **w/**  $T$

# LABOR MARKETS – STRUCTURE AND POLICY

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- ❑ Calibrate **exogenous policy** economy to hit empirical volatility of
  - ❑  $ue$ ,  $lfp$ , and  $\eta(\varepsilon)$
  
- ❑ Requires distortionary structural parameters

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- ❑ Labor tax rate smoothing not optimal in either selection model...

	Labor Selection		Walrasian
Relative SD (wrt GDP)	1.0		$\approx 0$ (CCK 1999, Werning 2007 QJE, many others)



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- ❑ ...or in matching model

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Relative SD (wrt GDP)	1.0	5.6  (Arseneau and Chugh 2012 <i>JPE</i> )	$\approx 0$  (CCK 1999, Werning 2007 <i>QJE</i> , many others)

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- ❑ Hiring subsidies large in long-run –  $\tau^h = 81\%$
- ❑ Hiring subsidies volatile in business cycles
- ❑ Economic difference vs. Walrasian labor markets?

# LABOR MARKETS – MODEL-CONSISTENT WEDGES

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- **Technological primitives**
  
- **Develop selection-model consistent transformation function and MRTs**
  - **Aggregate goods production technology**
  - **Aggregate matching technology**
  
- ⇒ **model-consistent decentralized wedges**
  
- **Tax volatility ⇒ EFFICIENT fluctuations**
  - **Selection model wedge fluctuations EXACTLY = 0**

# LABOR MARKETS – MODEL-CONSISTENT WEDGES

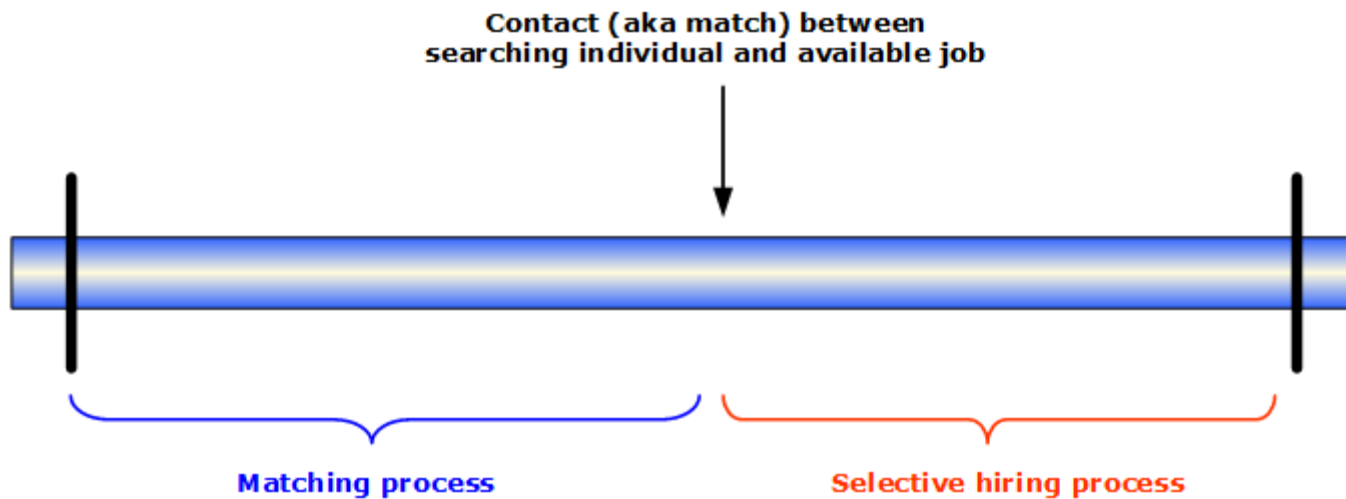
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⇒ **model-consistent decentralized wedges**
- ❑ **Tax volatility ⇒ EFFICIENT fluctuations**
  - ❑ **Selection model wedge fluctuations EXACTLY = 0**
- ❑ **Analytically characterize source of externalities**
  - ❑ **Cost gap = marginal hiring cost – avg. hiring cost**
- ❑ **“Selection Market Tightness”**
  - ❑ **Play highly similar role as market tightness externalities in matching model**
- ❑ **Compare and contrast with search and matching model**

# LABOR MARKETS – MATCHING VS. SELECTION

- **Matching** and **selection** two distinct components of recruiting process

↑  
"match quality"

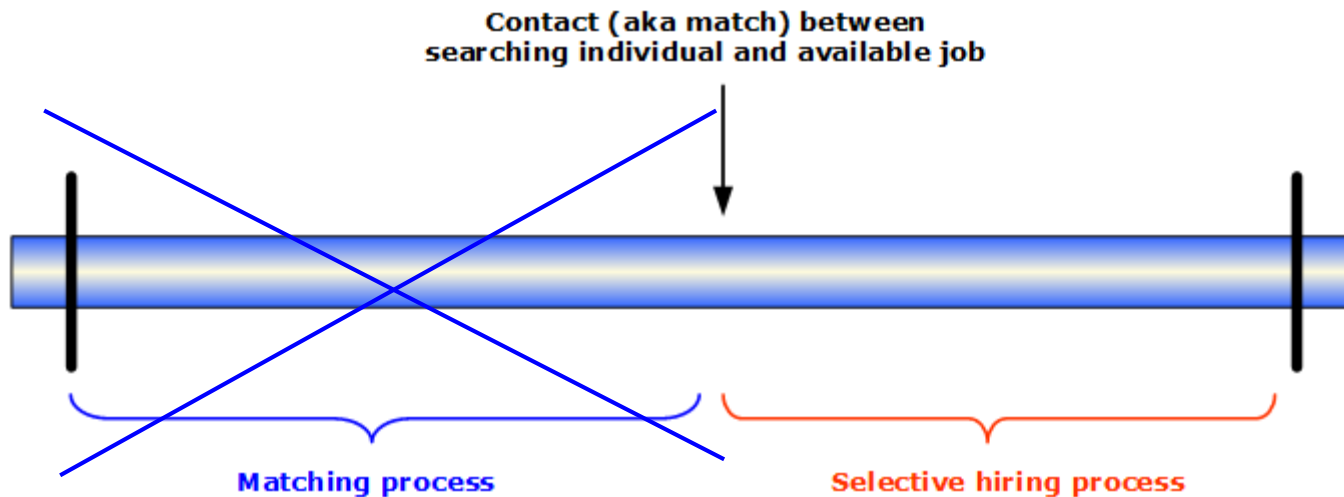


# LABOR MARKETS – MATCHING VS. SELECTION

- ❑ ~~Matching~~ and **selection** two distinct components of recruiting process

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- ❑ Components of recruiting costs
  - ❑ **Vacancy posting costs**
  - ❑ **Screening costs**
  - ❑ **Training costs**



# CONTRIBUTION TO LABOR & POLICY LITERATURES

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- ❑ **Need to know appropriate “wedges” for designing optimal policy**
  - ❑ **Fiscal policy**
  - ❑ **Monetary policy**
  - ❑ **Regulatory policy**
  
- ❑ **Recent literature on labor selection**
  - ❑ **Lechthaler, Merkl, and Snower (2010 *JECD*)**
  - ❑ **Merkl and van Rens (2012)**
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  - ❑ **Chugh and Merkl (2016 *IER*)**
  - ❑ **Faia, Lechthaler, and Merkl (2014 *JMCB*) (optimal monetary policy)**
  - ❑ **Baydur (2017 *AEJ: Macro*) – partial match quality revelation**

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- ❑ **Previous work**
  - ❑ **Arseneau, Chahrour, Chugh, Finkelstein Shapiro (2015 *JMCB*) (customer matching)**
  - ❑ **Chugh and Ghironi (2015) (endogenous product varieties)**
  - ❑ **Arseneau and Chugh (2012 *JPE*)**
  - ❑ **Aruoba and Chugh (2010 *JET*) (new monetarist)**
  - ❑ **Arseneau and Chugh (2008 *JME*) (nominal wage rigidities in labor matching model)**



# OUTLINE

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- ❑ **Model – Structure of Labor Markets**
- ❑ **GE efficiency – definitions of model-consistent wedges**
  - ❑ Extended model (**labor search and matching** + **labor selection**)
  - ❑ Focus on **labor selection** model (this paper)
- ❑ **Positive analysis (non-Ramsey policy)**
- ❑ **Ramsey equilibrium**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
- ❑ **Compare and contrast with search and matching model**
  - ❑ Implications for Beveridge Curve
  - ❑ Wage determination
  - ❑ Model-consistent wedges and “market tightness”
- ❑ **Conclusion**

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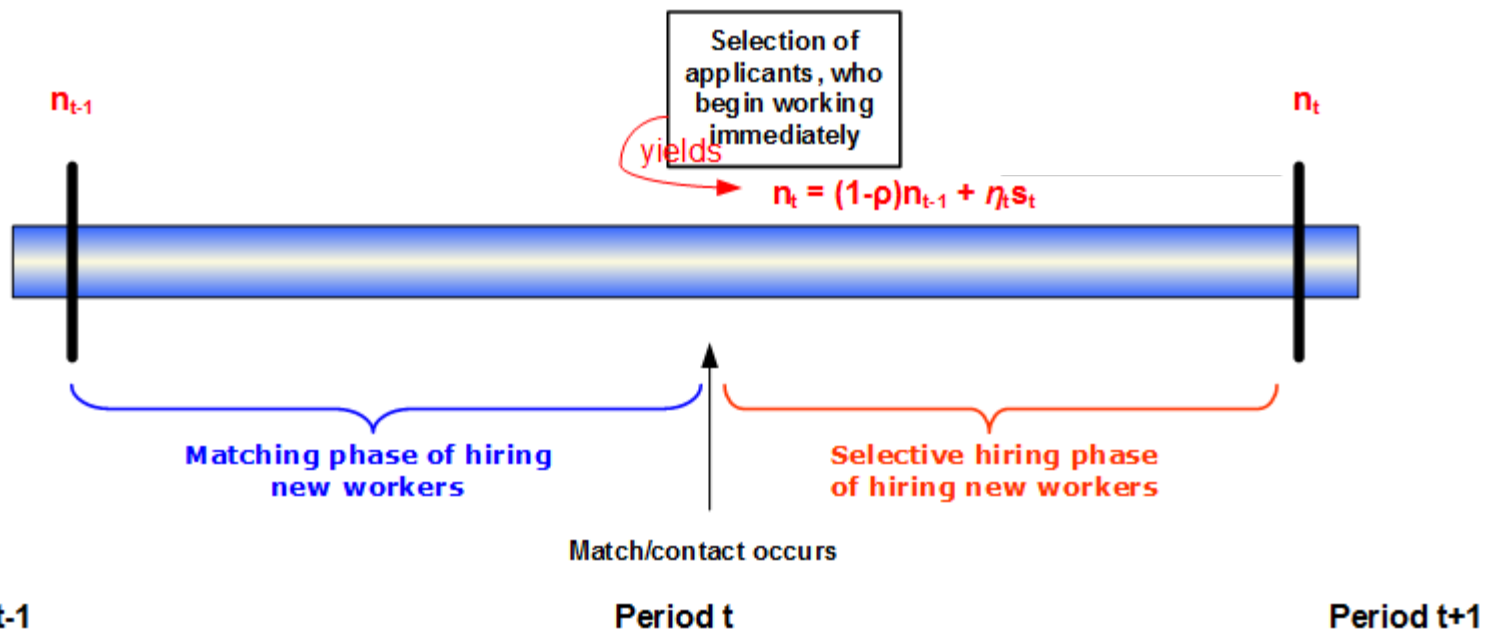
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# LABOR MARKET STRUCTURE

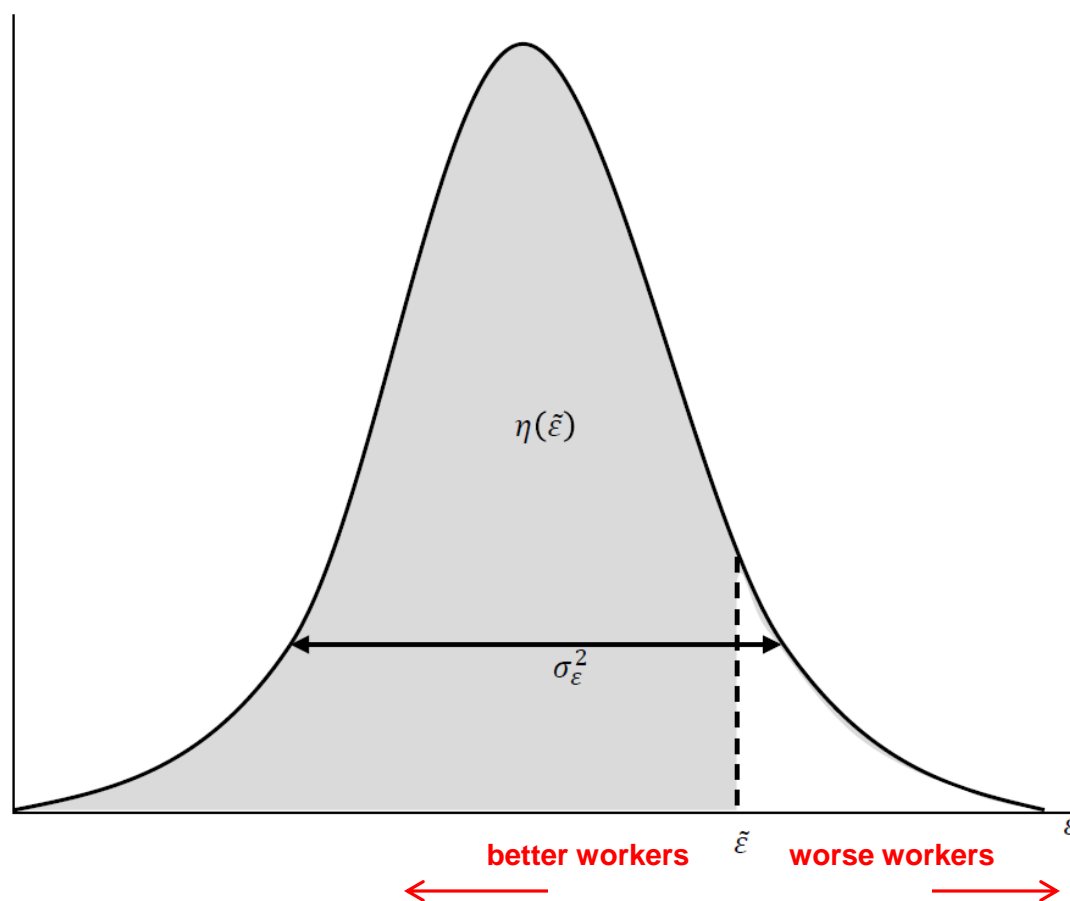
- ❑ Matching and **selection** two distinct concepts of frictional labor markets

↑  
"match quality"



# LABOR MARKET STRUCTURE

- Distribution of idiosyncratic hiring costs  $\varepsilon_i$



# LABOR MARKET STRUCTURE

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- $\tilde{\varepsilon}_t$       **endogenous selection threshold**
- $\eta(\tilde{\varepsilon}_t)$       **endogenous selection probability**
- $\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$       **average training cost for all newly-selected employees**
- $\sigma_\varepsilon$       **cross-sectional SD of training cost distribution**
- $v_t$       **vacancies**
- $k_t^h$       **matching probability for actively searching individual**
- $\gamma$       **vacancy posting cost**
- $m(s_t, v_t)$       **aggregate matching function**

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# MATCHING + SELECTION EFFICIENCY

□ **Social Planner**

$$\max_{\{c_t, n_t, s_t, \tilde{\epsilon}_t, v_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)]$$

$lfp_t \equiv (1 - \eta(\tilde{\epsilon}_t)k_t^h)s_t + n_t$

**s.t.**

$$c_t + g_t + \frac{H(\tilde{\epsilon}_t)}{\eta(\tilde{\epsilon}_t)} \cdot \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t) + \gamma v_t = z_t n_t$$

**Goods resource constraint**

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\epsilon}_t) \cdot m(s_t, v_t)$$

**Aggregate LOM for total employment**

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**Efficient LFP**

$$\frac{h'(lfp_t)}{u'(c_t)} = m_s(s_t, v_t) \cdot [\tilde{\epsilon}_t \cdot \eta(\tilde{\epsilon}_t) - H(\tilde{\epsilon}_t)]$$

**Efficient vacancy creation**

$$\frac{\gamma}{m_v(s_t, v_t)} = \tilde{\epsilon}_t \cdot \eta(\tilde{\epsilon}_t) - H(\tilde{\epsilon}_t)$$

... rewrite in terms of model-consistent wedges ...

**Intertemporal Efficiency**

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1 - \rho) [\tilde{\epsilon}_{t+1} - m_s(s_{t+1}, v_{t+1}) (\tilde{\epsilon}_{t+1} \eta(\tilde{\epsilon}_{t+1}) - H(\tilde{\epsilon}_{t+1}))]}{\tilde{\epsilon}_t - z_t}$$



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**Efficient LFP – identical to Arseneau and Chugh 2012 JPE (p. 949, eqn. 21)**

$$\frac{h'(lfp_t)}{u'(c_t)} = \frac{g \times m_s(s_t, v_t)}{m_v(s_t, v_t)}$$

**MRT between non-participation and output**

## Intertemporal Efficiency

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1 - \rho) \left[ \tilde{\epsilon}_{t+1} - m_s(s_{t+1}, v_{t+1}) (\tilde{\epsilon}_{t+1} \eta(\tilde{\epsilon}_{t+1}) - H(\tilde{\epsilon}_{t+1})) \right]}{\tilde{\epsilon}_t - z_t}$$

**IMRT: quantity of  $c_{t+1}$  that can be produced by reducing  $c_t$  by one unit, all else equal, by accumulating "wealth" in form of employment**

# SELECTION EFFICIENCY

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**Aggregate LOM for total employment**

□  $\gamma = 0$  **zero vacancy posting cost**

□  $m(s_t, v_t) = s_t^\xi v_t^{1-\xi}$  **trivial matching function**

↓ if  $\xi = 1$

$$m(s_t, v_t) = s_t$$

**Crucial obs. #1 for decentralized efficiency**

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Derivation in Appendix D based on transformation frontier

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# OVERVIEW

- ❑ **Infinitely-lived representative household, measure one of members**
  - ❑ **Full consumption insurance amongst – i.e., risk-sharing**
    - ❑ **Employed members**
    - ❑ **Unemployed members**
    - ❑ **Members outside the labor force (“leisure”)**
  - ❑ **Labor income taxation**
  - ❑ **Government-provided hiring subsidies**
  - ❑ **Government-provided unemployment benefits**
  - ❑ **Individual-specific Nash bargaining for newly-hired worker with  $\varepsilon_i$**
  - ❑ **Only an extensive labor margin, no intensive labor margin**
  - ❑ **Long-lasting labor-market relationships – exogenous separation rate  $\rho$**
- } Guarantees completeness of tax instruments (Ramsey issue)

# FIRMS

- **Production**
  - **New job  $i$  produces  $y_{it} = z_t - \varepsilon_{it}$  (output – hiring cost)**
  - **Hiring costs subsidized at rate  $\tau^h$**
  - **(Each incumbent job produces  $y_t = z_t$ )**

	<b>New hires</b>	<b>Avg. hiring costs</b>	<b>Avg. wage for new workers</b>	<b>Marg. wage for threshold new worker</b>	<b>Wage for incumbent worker</b>	<b>“Tightness”</b>
	$n_t^{NEW} = \eta(\tilde{\varepsilon}_t) s_t$	$\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$	$\frac{\omega_e(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}$	$w(\tilde{\varepsilon}_t)$	$w_t^I$	$\tilde{\varepsilon}_t \cdot \eta(\tilde{\varepsilon}_t) - H(\tilde{\varepsilon}_t)$

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- **Selection condition (aka labor demand) condition**

$$(1 - \tau_t^h) \cdot \tilde{\varepsilon}_t = z_t - w(\tilde{\varepsilon}_t) + (1 - \rho) E_t \left\{ \Xi_{t+1} \left[ (1 - \tau_{t+1}^h) \cdot \tilde{\varepsilon}_{t+1} + w(\tilde{\varepsilon}_{t+1}) - w_{t+1}^I \right] \right\}$$

**Cost of hiring = expected payoff of hiring**

- **Given individualistic wage setting, holds for every new worker**

$$(1 - \tau_t^h) \cdot \varepsilon_{it} = z_t - w(\varepsilon_{it}) + (1 - \rho) E_t \left\{ \Xi_{t+1} \left[ (1 - \tau_{t+1}^h) \cdot \tilde{\varepsilon}_{t+1} + w(\tilde{\varepsilon}_{t+1}) - w_{t+1}^I \right] \right\}$$



# HOUSEHOLD OPTIMIZATION

- Maximize expected lifetime utility

$$\max_{\{c, n_t, s_t, b_{it}\}} E_0 \sum_{t=0}^{\infty} \beta^t \left[ u(c_t) - \underbrace{h((1-\eta_t)s_t + n_t)}_{\text{disutility of participation}} \right]$$

s.t.

$$c_t + \sum_j \frac{1}{R_t^j} b_{t+1}^j = \underbrace{(1-\rho)n_{t-1} \cdot (1-\tau_t^n)w_t^I}_{\text{wages for measure of incumbent employees}} + \underbrace{(1-\tau_t^n) \cdot \left( \frac{\omega_{et}}{\eta_t} \right) \cdot \eta_t \cdot s_t}_{\text{wages for measure of newly-hired employees}} + \underbrace{(1-\eta_t)s_t\chi + b_t}_{\text{ue benefits for unemployed}} + \underbrace{(1-\tau^{pr})\Pi_t}_{\text{aggregate flow dividends received lump sum}}$$

**View  $\chi$  as fixed institutional parameter, not a cyclical policy choice**

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View  $\chi$  as fixed institutional parameter, not a cyclical policy choice

$$n_t = \underbrace{(1-\rho)n_{t-1}}_{\text{(exogenous) measure of pre-existing employment relationships terminate}} + \underbrace{\eta_t s_t}_{\text{flow of new employment relationships = measure of searchers } s_t \times \text{probability a searcher successfully lands a job}}$$

Perceived LOM for employment ("instantaneous production")

(exogenous) measure of pre-existing employment relationships terminate      flow of new employment relationships = measure of searchers  $s_t$  x probability a searcher successfully lands a job

FOCs  
↓

# HOUSEHOLD OPTIMIZATION

- **Optimal labor force participation (aka labor supply) condition**

$$\frac{h'(lfp_t)}{u'(c_t)} = \eta_t \left[ (1 - \tau_t^n) \left( \frac{\omega_{et}}{\eta_t} \right) + (1 - \rho) E_t \left\{ \Xi_{t+1|t} \left[ (1 - \tau_{t+1}^n) w_{t+1}^I + \frac{\mu_{ht+1}}{u'(c_{t+1})} \right] \right\} \right] + (1 - \eta_t) \chi$$

Envelope condition of period  
t+1 hh-level problem  
↓

- **Equates MRS cost with expected payoff of participation**

$$\begin{aligned} &\downarrow \quad \rho = 1 \\ &\downarrow \quad \chi = 1 \\ &\downarrow \quad \eta = 1 \end{aligned}$$

$$\frac{h'(lfp_t)}{u'(c_t)} = (1 - \tau_t^n) \omega_{et}$$

**Nests RBC labor supply function**

# WAGES

---

- **Surplus sharing** via individualistic Nash bargaining power
  - Newly-hired employee bargaining power =  $\alpha^E$
  - Incumbent employee bargaining power =  $\alpha^I$

# WAGES

## □ Surplus sharing via individualistic Nash bargaining power

- Newly-hired employee bargaining power =  $\alpha^E$
- Incumbent employee bargaining power =  $\alpha^I$

$$w(\tilde{\varepsilon}_t) = \frac{\chi}{1 - \tau_t^n} + \text{PDV}_t$$

Wage for marginal  
new worker

$$w(\varepsilon_{it}) = \frac{\chi}{1 - \tau_t^n} + \alpha^E (1 - \tau_t^h)(\tilde{\varepsilon}_t - \varepsilon_{it}) + \text{PDV}_t$$

Wage for infra-  
marginal new  
worker  $\varepsilon_{it}$

# WAGES

## □ Surplus sharing via individualistic Nash bargaining power

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$$w(\varepsilon_{it}) = \frac{\chi}{1 - \tau_t^n} + \alpha^E (1 - \tau_t^h) (\tilde{\varepsilon}_t - \varepsilon_{it}) + \text{PDV}_t$$

Wage for infra-marginal new worker  $\varepsilon_{it}$

$$\frac{\omega_e(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} = \frac{\chi}{1 - \tau_t^n} + \alpha^E (1 - \tau_t^h) \underbrace{\left( \tilde{\varepsilon}_t - \frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} \right)}_{\text{"Tightness"}} + \text{PDV}_t$$

Conditional average wage for all new workers

$$w_t^I = \frac{\chi}{1 - \tau_t^n} + \alpha^I (1 - \tau_t^h) \tilde{\varepsilon}_t + \text{PDV}_t$$

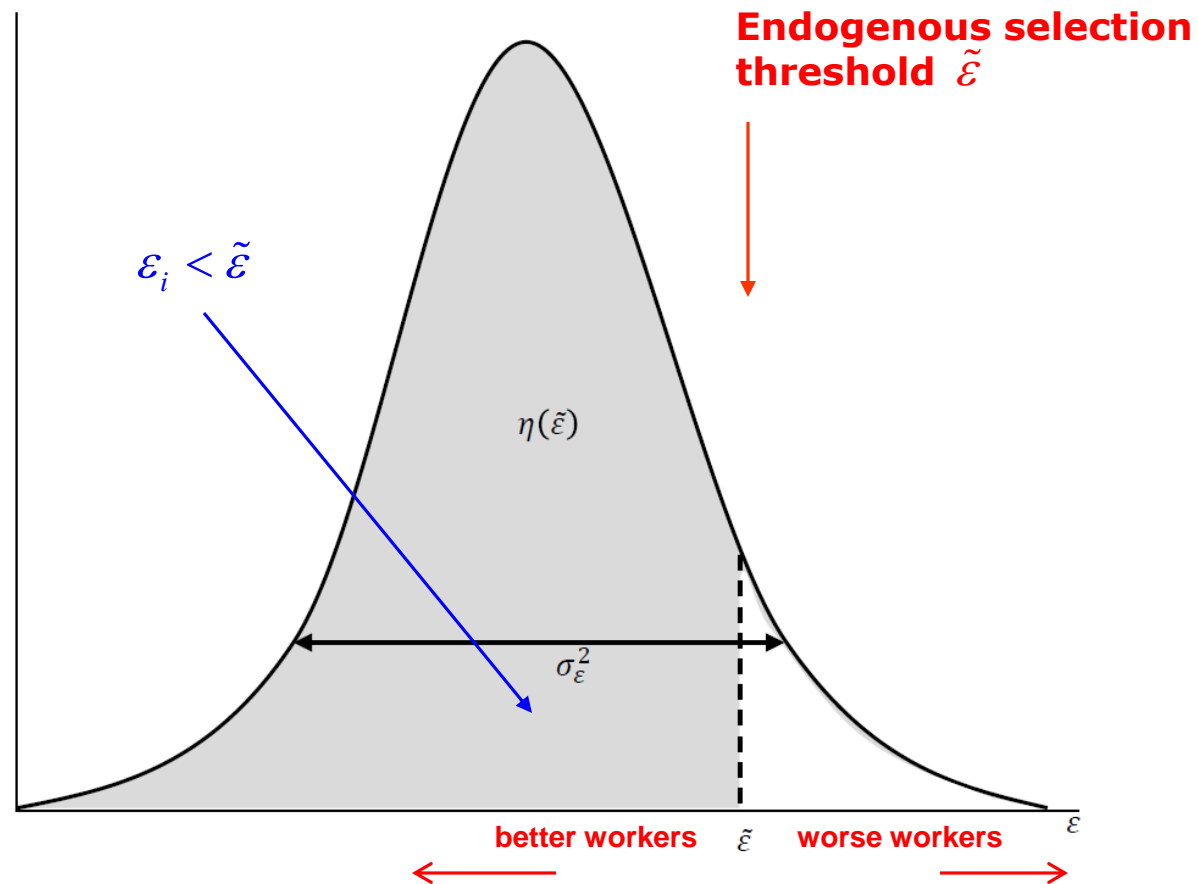
Wage for incumbent worker

## □ Endogenous wage dispersion

- Within newly-hired employees
- Across newly-hired employees and incumbent employees

# WAGES

- Distribution of idiosyncratic hiring costs  $\varepsilon_i$



# GOVERNMENT AND RESOURCE FRONTIER

- **Government**
  - **Government spending**
  - **Labor income tax**
  - **Hiring subsidies**
  - **Provision of ue benefits**
  - **One-period state contingent real debt**

- **Aggregate goods resource constraint**

$$c_t + g_t + \left( \frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} \right) \eta(\tilde{\varepsilon}_t) s_t = z_t n_t$$

- **Aggregate LOM for labor**

$$n_t = (1 - \rho) n_{t-1} + \eta(\tilde{\varepsilon}_t) s_t$$



# PRIVATE-SECTOR EQUILIBRIUM

- **State-contingent stochastic processes**  $\{c_t, n_t, s_t, \tilde{\varepsilon}_t, w_t^l, w(\tilde{\varepsilon}_t), \omega_e(\tilde{\varepsilon}), R_t^j\}_{t=0}^{\infty}$  that satisfy
  - **Household's bond Euler equations**
  - **LFP condition**
  - **Selective hiring condition**
  - **Nash wage outcomes**
  - **Law of motion for employment**  $n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\varepsilon}_t)s_t$
  - **Government budget constraint (key condition in Ramsey models)**
  - **Goods resource constraint**  $c_t + g_t + \left(\frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)}\right)\eta(\tilde{\varepsilon}_t)s_t = z_t n_t$
  - **Given processes**  $\{g_t, z_t, \tau_t^n, \tau_t^h\}_{t=0}^{\infty}$

# OUTLINE

---

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  - ❑ Focus on labor selection model
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- ❑ **Ramsey equilibrium**
- ❑ **Calibration**
- ❑ **Normative analysis (Ramsey policy) – wedge/distortion smoothing**
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**$\mathbf{X}_t$  is private-sector decision functions**

# RAMSEY PROBLEM

□ Ramsey problem – “Hybrid” Formulation

$$\max_{\{c_t, n_t, s_t, \tilde{\varepsilon}_t\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)] \quad lfp_t \equiv (1-\eta_t)s_t + n_t$$

s.t.

$$c_t + g_t + (H(\tilde{\varepsilon}_t) / \eta(\tilde{\varepsilon}_t)) \cdot \eta(\tilde{\varepsilon}_t) s_t = z_t n_t$$

Lagrange multiplier for each  $t$

PVIC

$$E_0 \sum_{t=0}^{\infty} \beta^t [u'(c_t) \cdot c_t - h'(lfp_t) \cdot lfp_t - u'(c_t) \cdot (1 - \tau^d) \cdot d_t] = A_0$$

Single Lagrange multiplier  $\mu$

# RAMSEY PROBLEM

□ Ramsey problem – “Hybrid” Formulation

$$\max_{\{c_t, n_t, s_t, \tilde{\varepsilon}_t, w(\tilde{\varepsilon}_t), w_t^I, \tau_t^n, \tau_t^h\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)] \quad lfp_t \equiv (1-\eta_t)s_t + n_t$$

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Lagrange multiplier for each  $t$

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$$E_0 \sum_{t=0}^{\infty} \beta^t [u'(c_t) \cdot c_t - h'(lfp_t) \cdot lfp_t - u'(c_t) \cdot (1 - \tau^d) \cdot d_t] = A_0$$

Single Lagrange multiplier  $\mu$

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\varepsilon}_t)s_t$$

$$\frac{h'(lfp_t)}{u'(c_t)} = \eta_t \left[ (1 - \tau_t^n) \left( \frac{\omega_{et}}{\eta_t} \right) + (1 - \rho) E_t \left\{ \Xi_{t+1|t} \left[ (1 - \tau_{t+1}^n) w_{t+1}^I + \frac{\mu_{ht+1}}{u'(c_{t+1})} \right] \right\} \right] + (1 - \eta_t) \chi$$

$$(1 - \tau_t^h) \cdot \tilde{\varepsilon}_t = z_t - w(\tilde{\varepsilon}_t) + (1 - \rho) E_t \left\{ \Xi_{t+1} \left[ (1 - \tau_{t+1}^h) \cdot \tilde{\varepsilon}_{t+1} + w(\tilde{\varepsilon}_{t+1}) - w_{t+1}^I \right] \right\}$$

# RAMSEY PROBLEM

□ Ramsey problem – “Hybrid” Formulation

$$\max_{\{c_t, n_t, s_t, \tilde{\varepsilon}_t, w_t^I, \tau_t^n, \tau_t^h\}} E_0 \sum_{t=0}^{\infty} \beta^t [u(c_t) - h(lfp_t)] \quad \text{If } lfp_t \equiv (1-\eta_t)s_t + n_t$$

s.t.

$$c_t + g_t + (H(\tilde{\varepsilon}_t) / \eta(\tilde{\varepsilon}_t)) \cdot \eta(\tilde{\varepsilon}_t) s_t = z_t n_t$$

Lagrange multiplier for each  $t$

PVIC

$$E_0 \sum_{t=0}^{\infty} \beta^t [u'(c_t) \cdot c_t - h'(lfp_t) \cdot lfp_t - u'(c_t) \cdot (1 - \tau^d) \cdot d_t] = A_0$$

Single Lagrange multiplier  $\mu$

$$n_t = (1 - \rho)n_{t-1} + \eta(\tilde{\varepsilon}_t)s_t$$

NOT captured in PVIC

$$\frac{h'(lfp_t)}{u'(c_t)} = \eta_t \left[ (1 - \tau_t^n) \left( \frac{\omega_{et}}{\eta_t} \right) + (1 - \rho) E_t \left\{ \Xi_{t+1|t} \left[ (1 - \tau_{t+1}^n) w_{t+1}^I + \frac{\mu_{ht+1}}{u'(c_{t+1})} \right] \right\} \right] + (1 - \eta_t) \chi$$

Lagrange multiplier for each  $t$

$$(1 - \tau_t^h) \cdot \tilde{\varepsilon}_t = z_t - w(\tilde{\varepsilon}_t) + (1 - \rho) E_t \left\{ \Xi_{t+1} \left[ (1 - \tau_{t+1}^h) \cdot \tilde{\varepsilon}_{t+1} + w(\tilde{\varepsilon}_{t+1}) - w_{t+1}^I \right] \right\}$$

$$w(\tilde{\varepsilon}_t) = \frac{\chi}{1 - \tau_t^n} + \text{PDV}_t \quad \frac{\omega_e(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} = \frac{\chi}{1 - \tau_t^n} + \alpha^E (1 - \tau_t^h) \left( \tilde{\varepsilon}_t - \frac{H(\tilde{\varepsilon}_t)}{\eta(\tilde{\varepsilon}_t)} \right) + \text{PDV}_t \quad w_t^I = \frac{\chi}{1 - \tau_t^n} + \alpha^I (1 - \tau_t^h) \tilde{\varepsilon}_t + \text{PDV}_t$$

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# CALIBRATION

- ❑ Parameterize so non-Ramsey economy generates empirically reasonable labor market fluctuations in  $ue$ ,  $lfp$ , and hiring rate  $\eta(\varepsilon)$
- ❑ Conditional on exogenous fluctuations in
  - ❑ Labor tax rate
  - ❑ Productivity
  - ❑ Government purchases
- ❑ **Crucial parameters – Part I**
  - ❑ **Distributional form** – logistic (also have used normal distribution)
  - ❑ Mean  $\mu_\varepsilon = 0.30$
  - ❑ **Cross-sectional standard deviation  $\sigma_\varepsilon = 0.19$**
- ❑ **Value of  $\sigma_\varepsilon$  disciplined by micro-level evidence**
  - ❑ **SD  $\sigma_\varepsilon$  across new hires of training costs = 207 hours ( = 40% of MPN)**
  - ❑ Barron, Black, and Loewenstein (1989 *JLE*)
  - ❑ Firm-level costs of interviewing/hiring/training new workers
  - ❑ Based on 1982 EOPP (Employment Opportunities Pilot Project)



# CALIBRATION

- ❑ **Parameterize so non-Ramsey economy generates empirically reasonable labor market fluctuations in  $ue$ ,  $lfp$ , and hiring rate  $\eta(\varepsilon)$**
- ❑ **Conditional on exogenous fluctuations in**
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  - ❑ **Mean  $\mu_\varepsilon = 0.30$**
  - ❑ **Cross-sectional standard deviation  $\sigma_\varepsilon = 0.19$**
- ❑ **Crucial parameters – Part II**
  - ❑ **Unemployment benefits = 0.70**
  - ❑ **Worker Nash bargaining power  $\alpha^E = \alpha^I = 0.50$** 
    - ❑ **For both new hires and incumbents**
- ❑ **Other parameters “standard” (Table 3)**

Crucial obs. #2 for  
decentralized efficiency

# DYNAMIC RESULTS

			<b>Non-Ramsey Policy (positive)</b>	<b>Data</b>
<b>Labor Tax Rate</b>	<b>Mean</b>		<b>20%</b>	<b>20%</b>
	<b>Rel. SD</b>		<b>0.98</b>	<b>1.8</b>
<b>“Tightness” ( <math>\varepsilon\eta(\varepsilon) - H(\varepsilon)</math> )</b>	<b>Rel. SD</b>		<b>5.58</b>	
<b>Hiring rate <math>\eta(\varepsilon)</math></b>	<b>Rel. SD</b>		<b>3.5</b>	<b>3.7</b>
<b>Unemployment</b>	<b>Rel. SD</b>		<b>8.6</b>	<b>5.2</b>
<b>LFP</b>	<b>Rel. SD</b>		<b>0.22</b>	<b>0.20</b>

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# DYNAMIC RESULTS

		Ramsey	Non-Ramsey Policy (positive)	Data
Labor Tax Rate	Mean	22%	20%	20%
	Rel. SD	0.98	0.98	1.8
"Tightness" ( $\varepsilon\eta(\varepsilon) - H(\varepsilon)$ )	Rel. SD	1.09	5.58	
Hiring rate $\eta(\varepsilon)$	Rel. SD	0.03	3.5	3.7
Unemployment	Rel. SD	5.3	8.6	5.2
LFP	Rel. SD	0.23	0.22	0.20

- ❑ Ramsey simulations: shocks to  $z, g$  conditional on structural parameters
- ❑ Observations
  1. Labor income tax rate smoothing **NOT** optimal
  2. Volatility of  $\eta(\varepsilon)$  **much** smaller than in data

# DYNAMIC RESULTS

		Ramsey Policy		Social Planner
		Baseline parameters		
Labor Tax Rate	Mean	22%		0%
	Rel. SD	0.99		0
"Tightness" ( $\varepsilon\eta(\varepsilon) - H(\varepsilon)$ )	Rel. SD	1.09		1.09
Hiring rate $\eta(\varepsilon)$	Rel. SD	0.03		0.03
Unemployment	Rel. SD	5.39		5.39
LFP	Rel. SD	0.04		0.04

- ❑ Social Planner simulations: shocks to  $z$
- ❑ Ramsey simulations: Inefficient structural parameters DO appear in problem
- ❑ **Efficient surplus sharing**

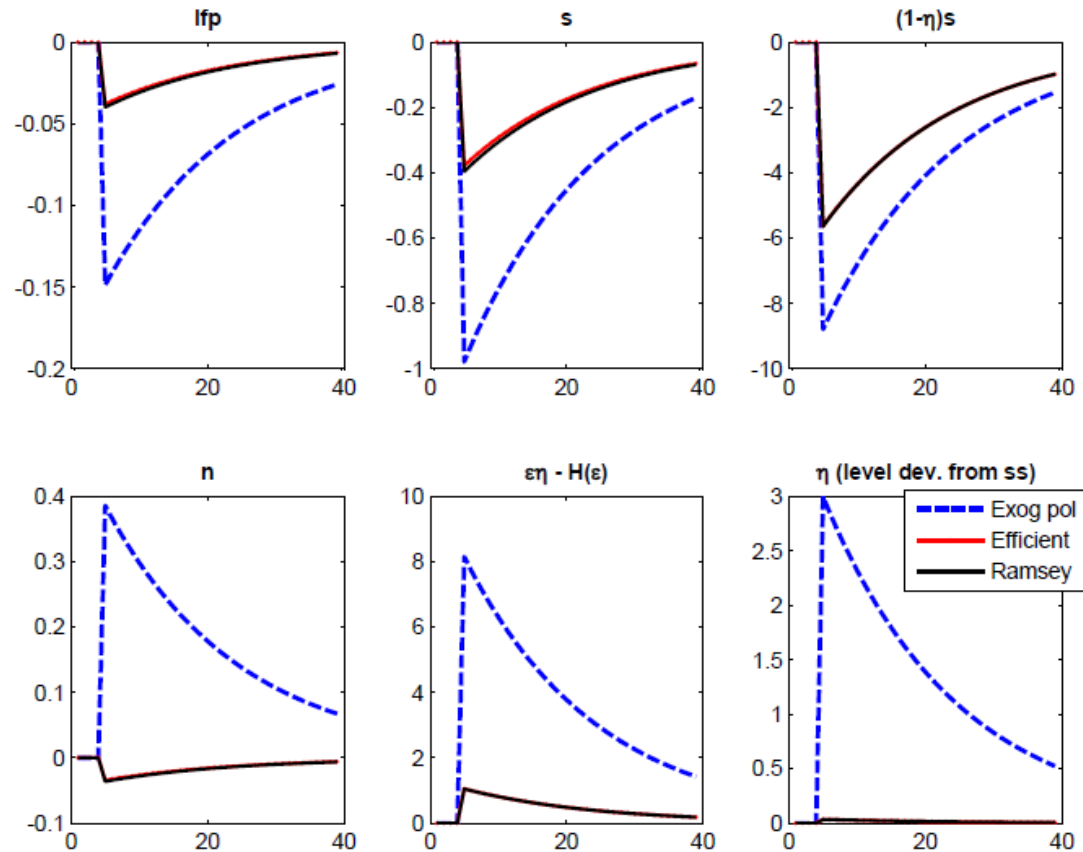
# DYNAMIC RESULTS

		Ramsey Policy		
		Baseline parameters	For ANY $(\alpha, \chi)$ pair	Social Planner
Labor Tax Rate	Mean	22%	---	0%
	Rel. SD	0.99	---	0
"Tightness" ( $\varepsilon\eta(\varepsilon) - H(\varepsilon)$ )	Rel. SD	1.09	1.09	1.09
Hiring rate $\eta(\varepsilon)$	Rel. SD	0.03	0.04	0.03
Unemployment	Rel. SD	5.39	5.39	5.39
LFP	Rel. SD	0.04	0.04	0.04

- ❑ Social Planner simulations: shocks to  $z$
- ❑ Ramsey simulations: Inefficient structural parameters DO appear in problem
- ❑ Efficient surplus sharing for ANY  $(\alpha, \chi)$  pair

# DYNAMIC RESULTS

## □ Impulse response to productivity



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# BEVERIDGE CURVE

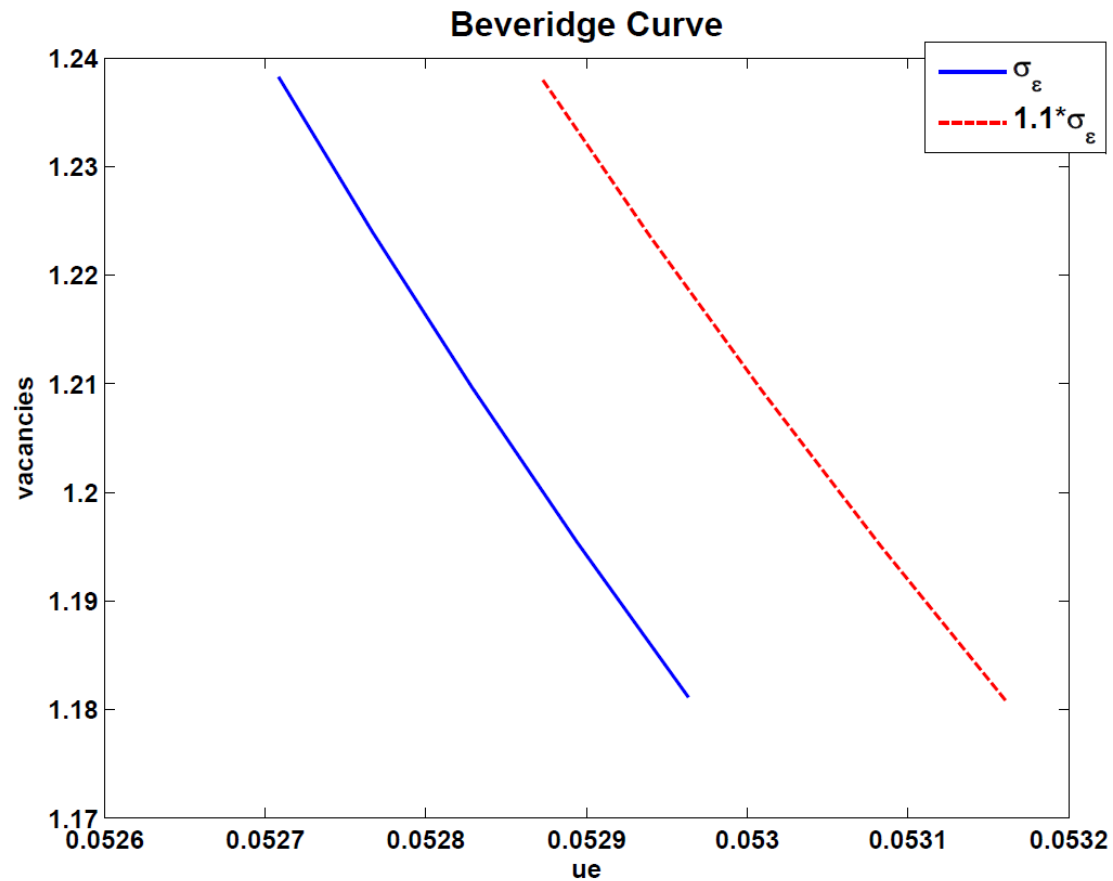
- ❑ **Outwards shift of Beveridge Curve during Great Recession**
  - ❑ **Elsby, Michaels, and Ratner (2015 *JEL*)**
  - ❑ **Diamond and Sahin (2014 *NY Fed Staff Report*)**
  
- ❑ **Reduced-form interpretation: “matching efficiency”  $\Omega$  has declined**

$$\Omega \cdot m(s_t, v_t)$$

- ❑ **Cheremukhin and Restrepo-Echavarria (2014 *EER*)**
  - ❑ **Pescatori and Tasci (2011)**
  - ❑ **Chahrour, Chugh, and Potter (2018)**
  
- ❑ **Proposal: increase in primitive cross-sectional SD  $\sigma_\varepsilon$** 
  - ❑ **Gets inside black-box  $\Omega$**
  - ❑ **(Distributional explanation at heart of Lester (2010 *JET*))**

# BEVERIDGE CURVE

- Outwards shift of Beveridge Curve during Great Recession



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# NASH BARGAINING & EFFICIENCY

- Suppose zero taxes in decentralized economy

- **Selection model (no search and matching)**

- **(Trivial matching function)**

$$\begin{aligned} m(s_t, v_t) &= s_t^\xi v_t^{1-\xi} && \text{(with } \xi = 1) \\ &= s_t \end{aligned}$$

- **Nash bargaining parameter  $\alpha^E = \xi = 1$  achieves efficient allocations**

- **Efficient surplus sharing**

# NASH BARGAINING & EFFICIENCY

- Suppose zero taxes in decentralized economy

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- **Nash bargaining parameter  $\alpha^E = \xi = 1$  achieves efficient allocations**

- **Efficient surplus sharing**

- **Search and matching model (no selection)**

- **Matching function (fundamental)**

$$m(s_t, v_t) = s_t^\xi v_t^{1-\xi} \quad \xi \in (0.3, 0.7)$$

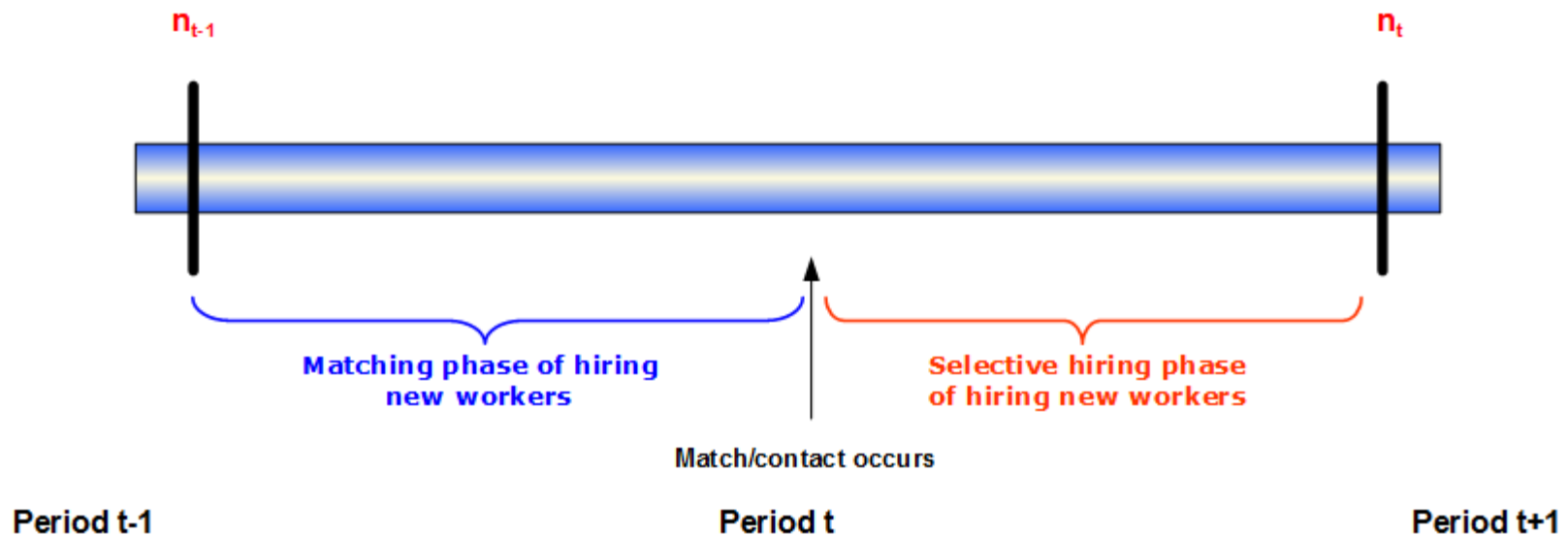
- **Nash bargaining parameter  $\alpha^E = \xi < 1$  achieves efficient allocations**

- **Hosios (1990) condition**

- **Efficient surplus sharing**

# NASH BARGAINING & EFFICIENCY

- ❑ Suppose zero taxes in decentralized economy
- ❑ **Matching** + **Selection**
- ❑ No value of  $\alpha^E$  can decentralize efficient surplus sharing
  - ❑ Two competing efficiency goals...
  - ❑ ...but only ONE wage determination mechanism



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# LABOR MARKETS – MODEL-CONSISTENT WEDGES

- ❑ Develop selection-model consistent transformation function and MRTs
  - ❑ Aggregate goods resource constraint
  - ❑ Aggregate law of motion of employment

⇒ model-consistent decentralized wedges

- ❑ Tax volatility ⇒ EFFICIENT fluctuations
  - ❑ Selection model wedge fluctuations EXACTLY = 0
- ❑ Analytically characterize source of externalities
  - ❑ Cost gap = marginal hiring cost – avg. hiring cost
- ❑ “Selection Market Tightness”
  - ❑ Play highly similar role as market tightness externalities in matching model

Efficient labor supply in matching model (Arseneau and Chugh 2012 JPE)

$$MRS_{c_t, n_t} = \gamma \cdot \left( \frac{\alpha}{1 - \alpha} \right) \cdot \theta_t$$

$$MRS_{c_t, n_t} = \tilde{\varepsilon}_t \cdot \eta(\tilde{\varepsilon}_t) - H(\tilde{\varepsilon}_t)$$

Efficient labor supply from Chugh and Merkl 2016 IER



# LABOR MARKETS

Efficient labor supply in matching model (Arseneau and Chugh 2012 JPE)

$$\frac{h'(lfp_t)}{u'(c_t)} = \underbrace{\gamma \cdot \left( \frac{\alpha}{1-\alpha} \right) \cdot \theta_t}_{\text{Within-period MRT}}$$

Within-period MRT

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left( \frac{\gamma}{(1-\alpha)\theta_{t+1}^{-\alpha}} - \gamma \cdot \frac{\alpha}{1-\alpha} \cdot \theta_{t+1} \right)}{\underbrace{\frac{\gamma}{(1-\alpha)\theta_t^{-\alpha}} - z_t}_{\text{Intertemporal MRT}}}$$

Intertemporal MRT

# LABOR MARKETS

Efficient labor supply in matching model (Arseneau and Chugh 2012 *JPE*)

$$\frac{h'(lfp_t)}{u'(c_t)} = \underbrace{\gamma \cdot \left( \frac{\alpha}{1-\alpha} \right) \cdot \theta_t}_{\text{Within-period MRT}}$$

Within-period MRT

$$\frac{h'(lfp_t)}{u'(c_t)} = \underbrace{\tilde{\epsilon}_t \cdot \eta(\tilde{\epsilon}_t) - H(\tilde{\epsilon}_t)}_{\text{Within-period MRT}}$$

Within-period MRT

Efficient labor supply in selection model (Chugh and Merkl 2016 *IER*)

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left( \frac{\gamma}{(1-\alpha)\theta_{t+1}^{-\alpha}} - \gamma \cdot \frac{\alpha}{1-\alpha} \cdot \theta_{t+1} \right)}{\frac{\gamma}{(1-\alpha)\theta_t^{-\alpha}} - z_t}$$

Intertemporal MRT

$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left( \tilde{\epsilon}_{t+1} - (\tilde{\epsilon}_{t+1} \eta(\tilde{\epsilon}_{t+1}) - H(\tilde{\epsilon}_{t+1})) \right)}{\tilde{\epsilon}_t - z_t}$$

Intertemporal MRT



Substitute intratemporal conditions into intertemporal conditions

# LABOR MARKETS

Marginal cost of hiring a new employee



$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left( \frac{\gamma}{(1-\alpha)\theta_{t+1}^{-\alpha}} - \frac{h'(lfp_{t+1})}{u'(c_{t+1})} \right)}{\frac{\gamma}{(1-\alpha)\theta_t^{-\alpha}} - z_t}$$

Marginal cost of hiring a new employee



$$\frac{u'(c_t)}{\beta u'(c_{t+1})} = \frac{(1-\rho) \left( \tilde{\epsilon}_{t+1} - \frac{h'(lfp_{t+1})}{u'(c_{t+1})} \right)}{\tilde{\epsilon}_t - z_t}$$

# CONCLUSIONS

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- ❑ **Selective hiring framework realistic**
- ❑ **Selective hiring costs are distinct from vacancy posting costs**
  - ❑ **Davis, Faberman, and Haltiwanger (2013 QJE):  $\approx 40\%$  of hiring costs are NOT vacancy posting costs**
- ❑ **Smoothing (model-consistent) wedges the goal for optimal policy**
  - ❑ **Not smoothing policy instruments**
- ❑ **Model-consistent wedges apply to**
  - ❑ **Fiscal policy**
  - ❑ **Monetary policy**
  - ❑ **Regulatory policy**